

Precision Spectroscopy of HCI in the Dark

Precision Spectroscopy of Atomic Quantum Levels without Detecting Emission of Photons or Electrons

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spare
Stored Particle Atomic Research Collaboration

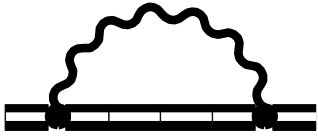
Stored Particle Atomic Research Collaboration

- Mass Measurements with High Precision in Penning Traps
- Resonant Coherent Excitation of Fast Ions in Crystals
- Collision Spectroscopy:
 - Q-value in Electron Capture Measured Precisely by COLTRIMS
 - Resonances in Electron Scattering by Dielectronic Recombination

Motivation:

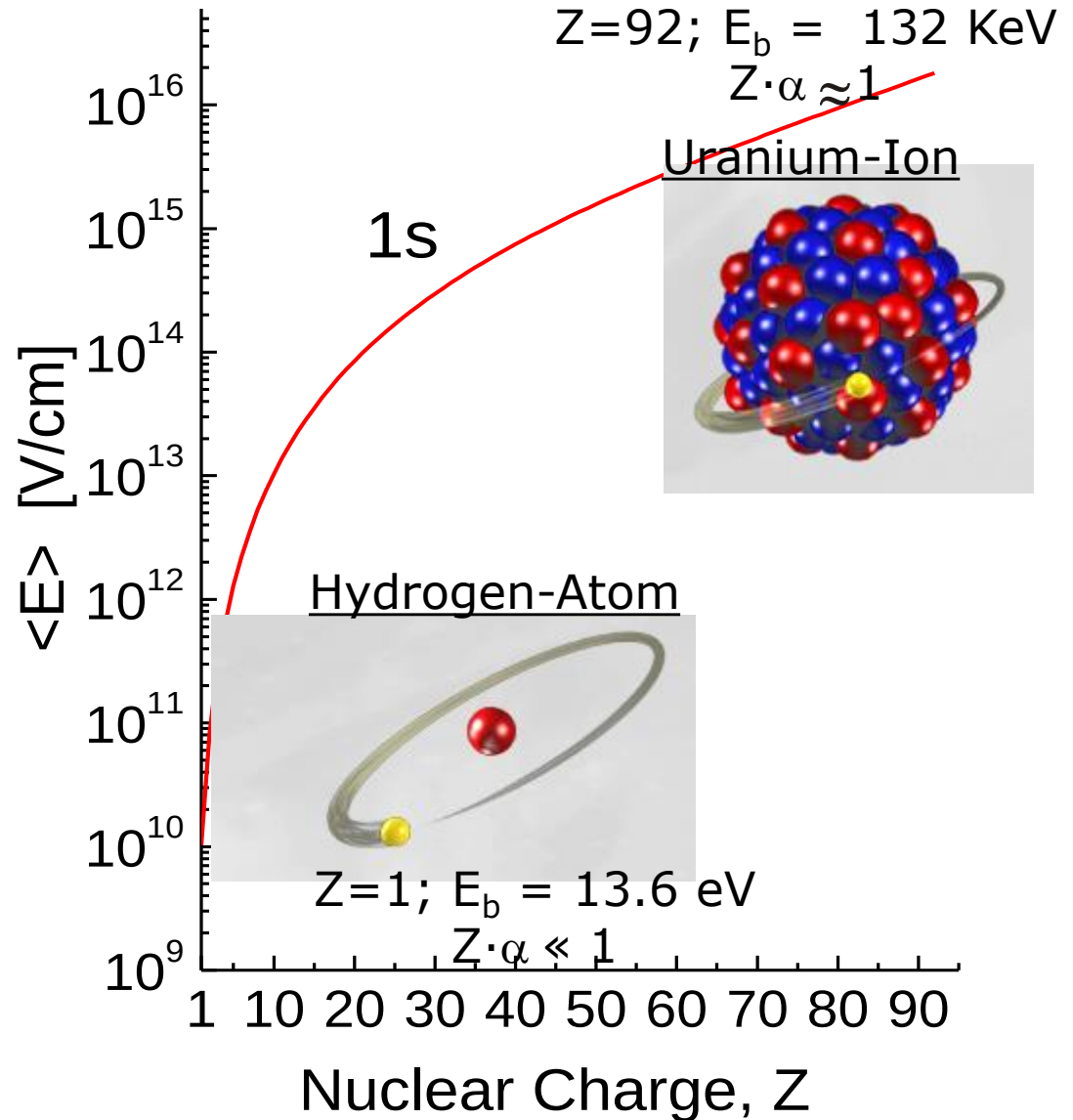
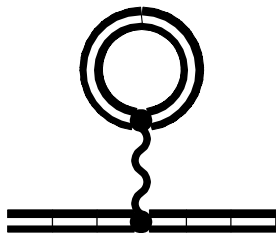
Atomic Physics in Extremely Strong Fields

Self Energy



Quantum
Electro-
Dynamics

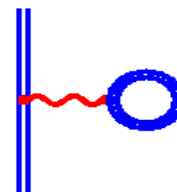
*Vacuum
Polarization*



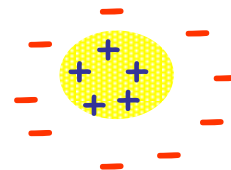
1s-ground state: increase of the electric field strength by six orders of magnitude

H-like "One Photon"

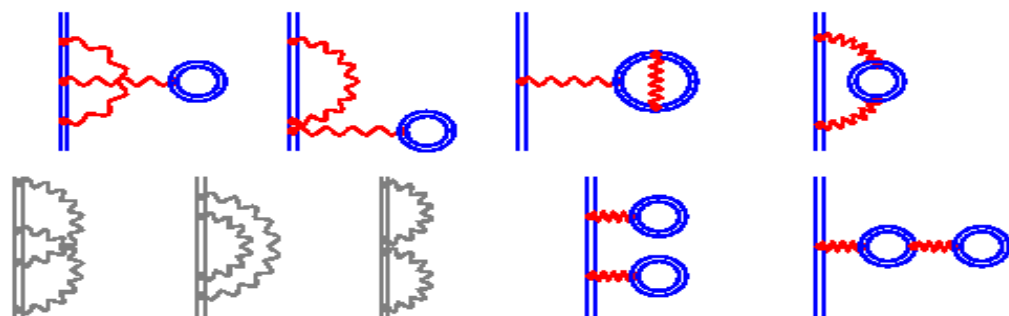
Self
Energy



Vacuum
Polarization

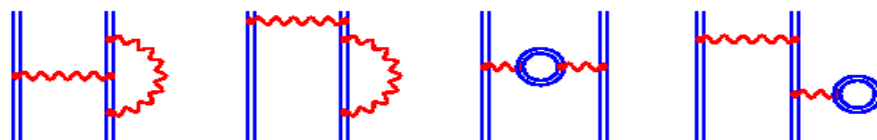


$m_{\text{bare}} \longrightarrow m_{\text{obs}}$



H-like ion "Two Photon"
QED

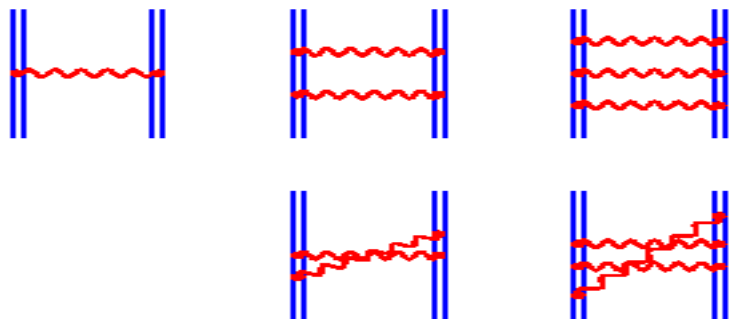
"Screening of S.E. and V. P."
for ions with several electrons



Relativistic Many-Body Perturbation
Theory (RMBPT)

Relativistic Configuration Interaction
(CI)

+ QED



● The structural aspect

The Problem: Many e⁻ (one - two - many!)

The Methods: Conservation of Misery

Strength

Weakness

● Configuration Interaction (CI)

Accuracy, strongly correlated systems

Scaling with # particles

$$\Psi = \sum_i \xi_i | \Phi_1 \Phi_2 \dots \Phi_N \rangle_i$$

● Multi-Configuration Hartree/Dirac-Fock

Versatile!
(FAC code)

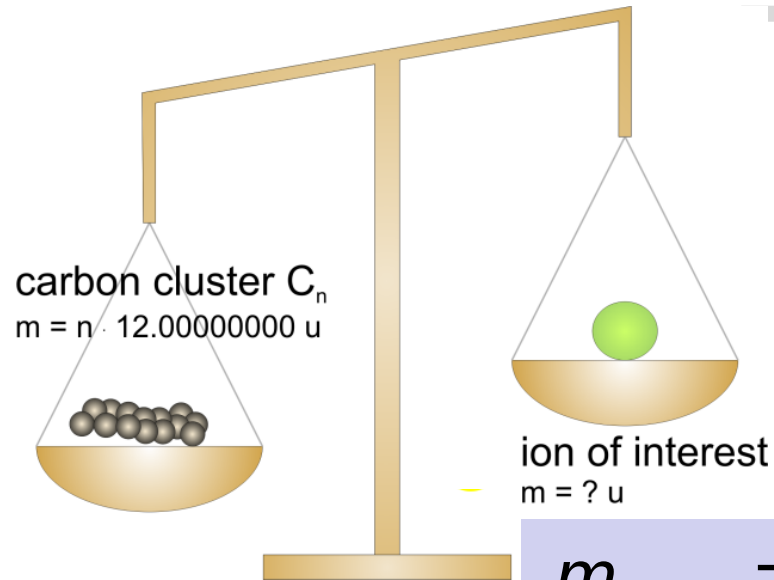
Core-polarization

● Perturbation Theory (RMPT) - Coupled Cluster

High accuracy for few e⁻ ions!

Starting point, tedious calculation

Mass Measurements with High Precision in Penning Traps for Binding Energy Determination



Using Einstein's $E = mc^2$, Confirmed to be correct to 0.00004% by Pritchard et al., in Trap (Nature 438, 1097 (2005))

$$m_{\text{Atom}} = N \cdot m_{\text{neutron}} + Z \cdot m_{\text{proton}} + Z \cdot m_{\text{electron}} - (B_{\text{atom}} + B_{\text{nucleus}})/c^2$$

$$\delta m/m < 10^{-10}$$

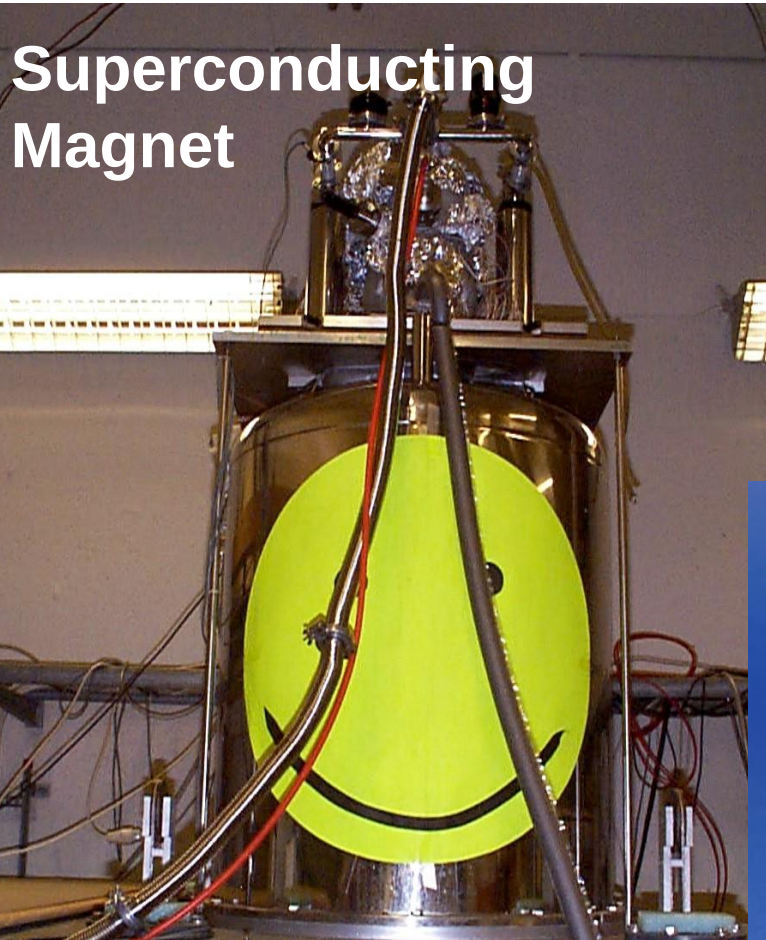
$$\delta m/m = 10^{-6} - 10^{-8}$$

change number of electrons by using highly charged ions in different charge states

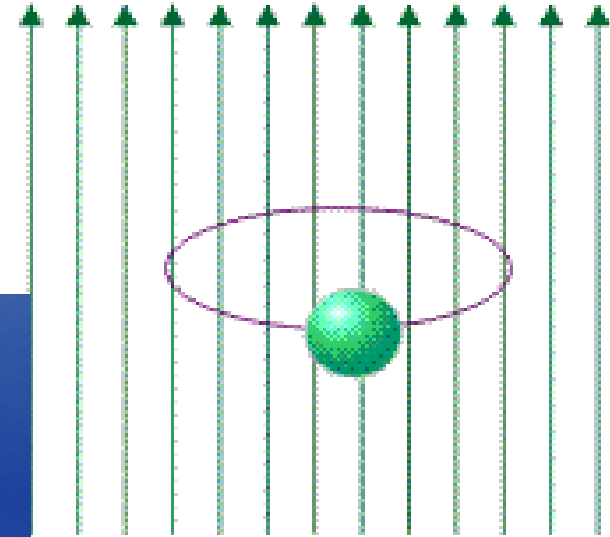
Keep B_{nucleus} fixed

High-precision mass measurements

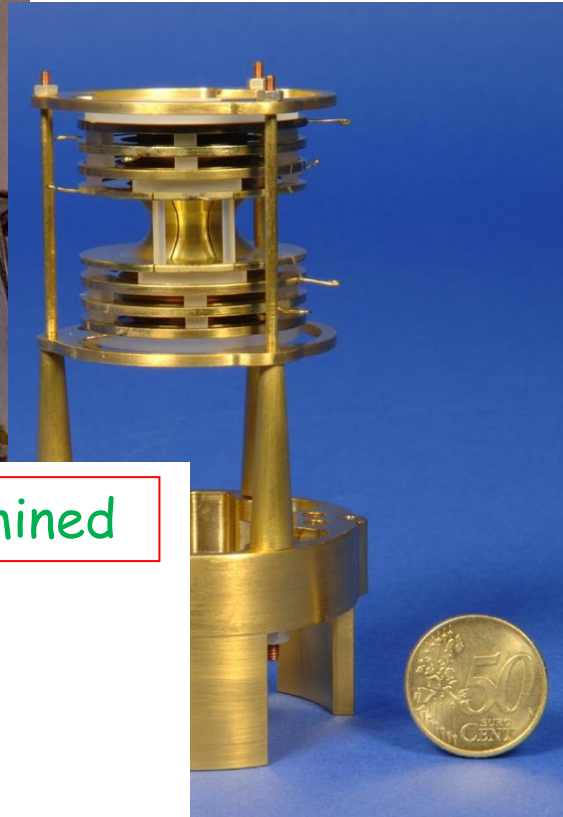
Superconducting Magnet



$\vec{B}$ • Cyclotron frequency

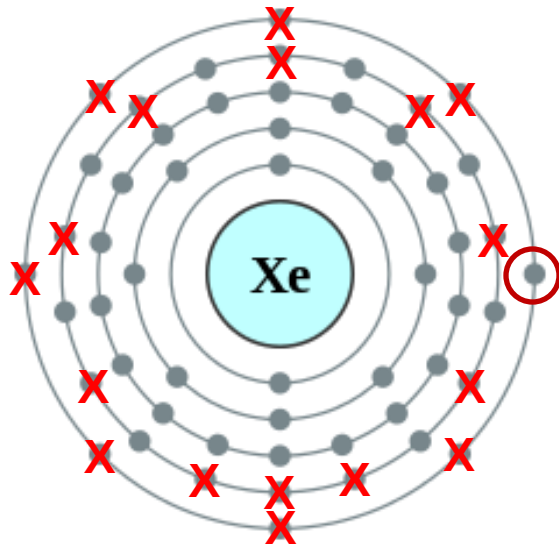


$$\frac{\omega_{\text{ref}}}{\omega_{\text{ion}}} = \frac{\overset{\text{known}}{q_{\text{ref}}} \overset{\text{determined}}{m_{\text{ion}}} B}{q_{\text{ion}} m_{\text{ref}} B}$$



$$\omega_c = \frac{q}{m} \cdot B$$

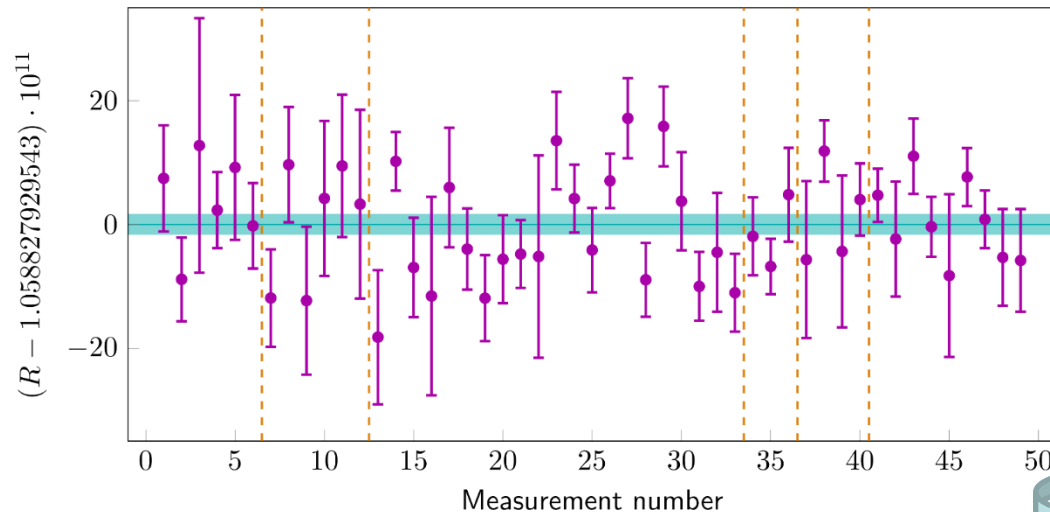
Weighing binding energies with PENTATRAP@MPIK



Electron configuration of Xenon ($Z = 54$):

$1s^2 2s^2 2p^6 3s^2 3p^6 4s^2 3d^{10} 4p^6 5s^2 4d^{10} 5p^6$
Neutral Xe atom $[\text{Kr}] 5s^2 4d^{10} 5p^6$

Measure the mass difference of Xe^{17+} and Xe^{18+}
yields the binding energy of the 18th electron.



PENTATRAP@MPIK:
 $\delta m/m_{\text{stat}} = 1.1 \cdot 10^{-11}$ ($\delta m \sim 1.4$ eV)

Exp.: $B(4d^1)_{\text{Xe}} = 432.4 (1.4)(3.4)$ eV

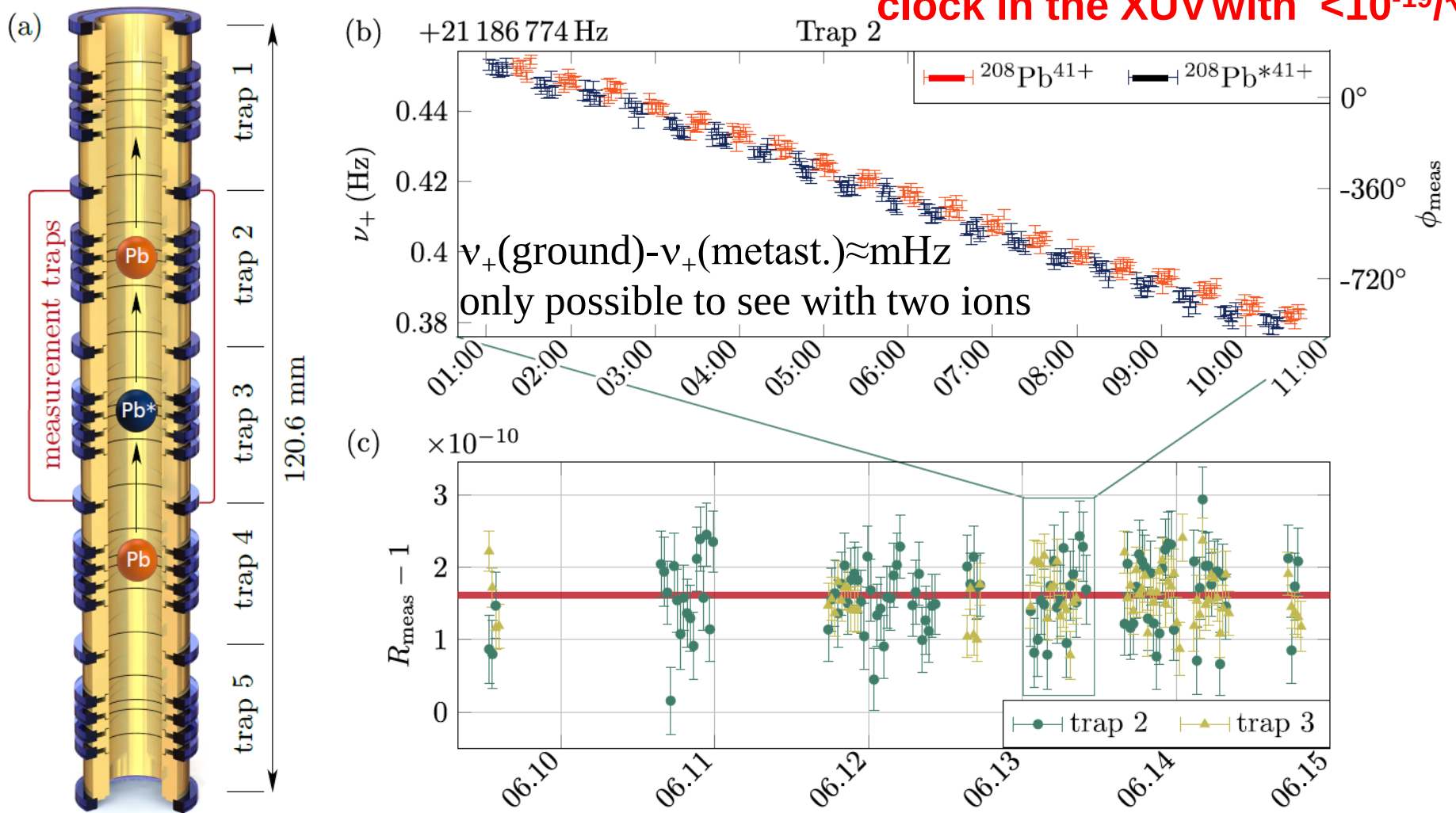
Theorie: $B(4d^1)_{\text{Xe}} = 432.4 (3.0)$ eV (PI)

$B(4d^1)_{\text{Xe}} = 435.1 (1.0)$ eV (ZH)

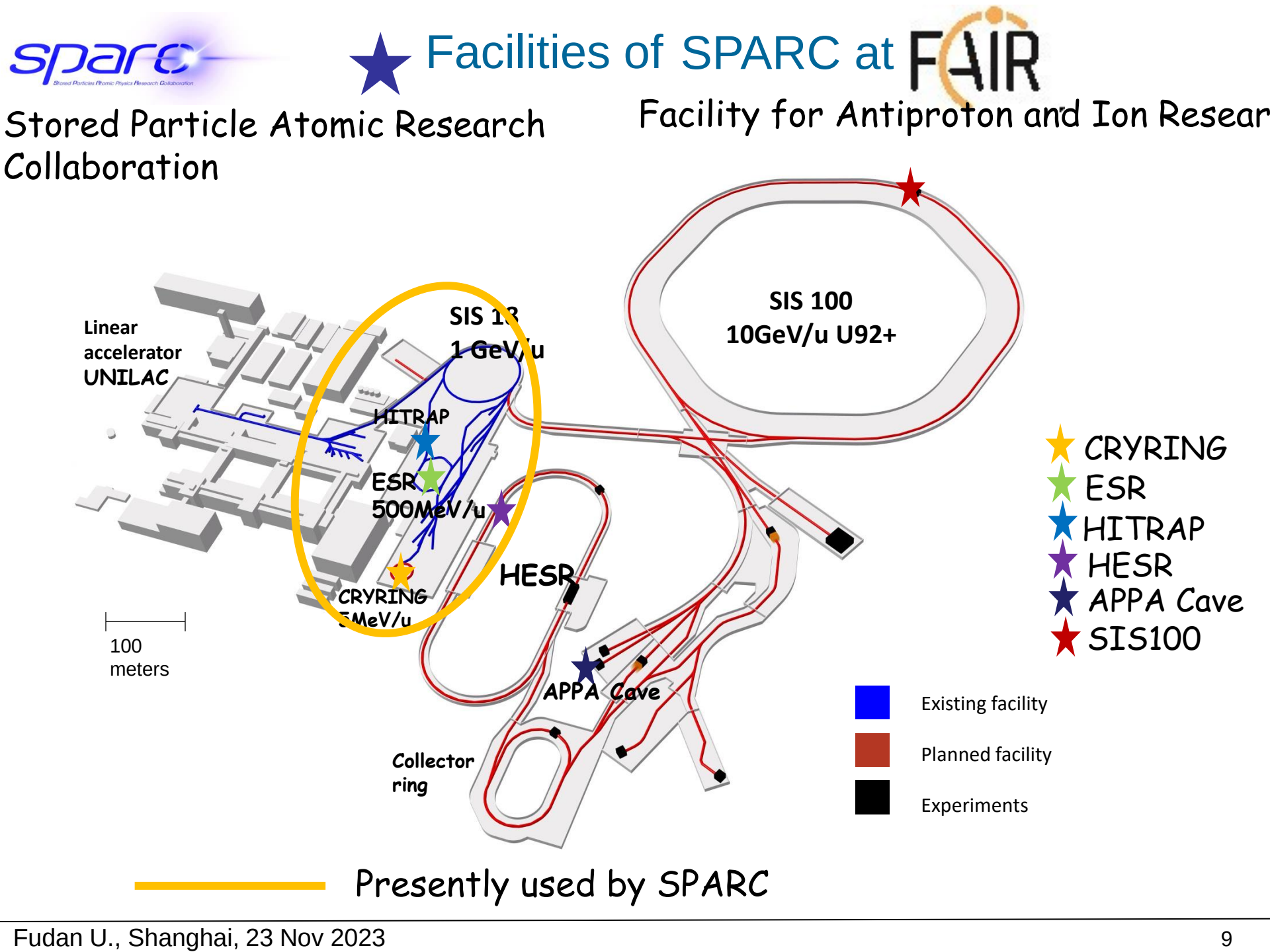
Test of many electron calculations

Weighing binding energies with PENTATRAP@MPIK

Low-lying metastable electronic state in $^{208}\text{Pb}^{41+} \rightarrow$ First step towards HCl clock in the XUV with $<10^{-19}/\sqrt{\tau}$



Ratio precision of $4 \cdot 10^{-12}$ $\Delta m = 31.2 \pm 0.8 \text{ eV} = \text{metastabl excitation energy}$
lifetime 26,5 d



HITRAP

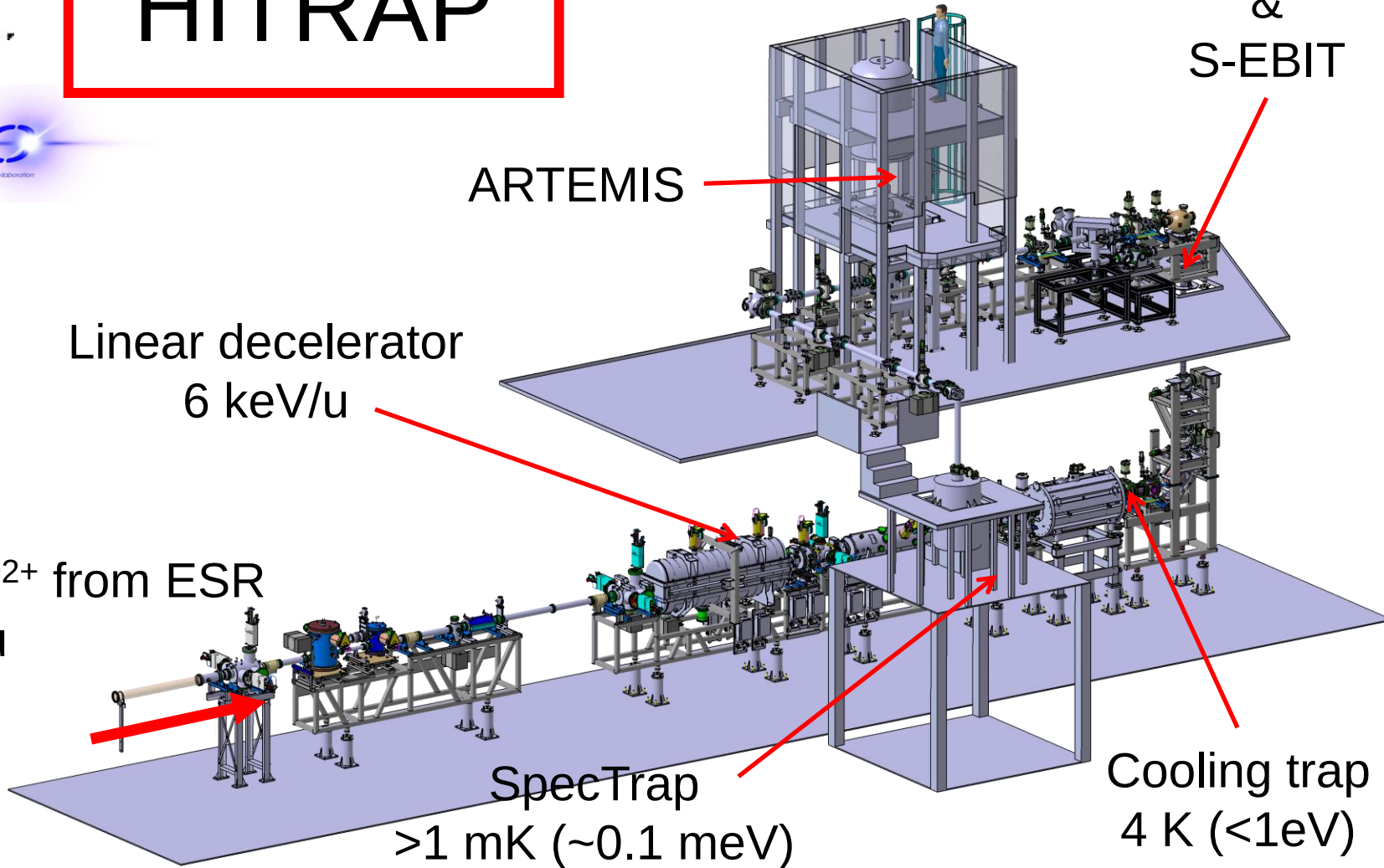
Presently commissioned

DR-EBIT
&
S-EBIT

ARTEMIS

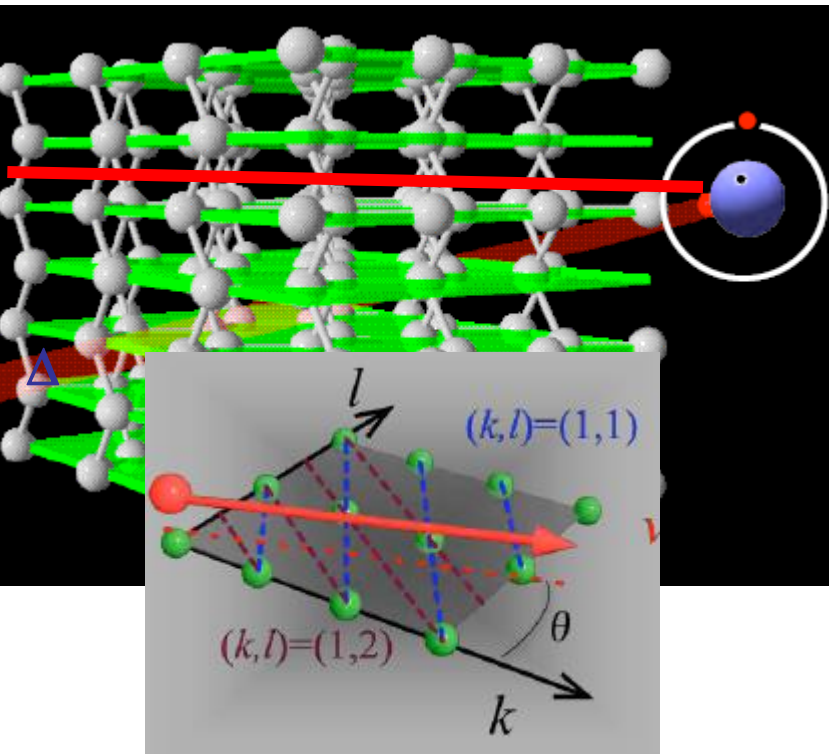
Linear decelerator
6 keV/u

up to U^{92+} from ESR
4 MeV/u

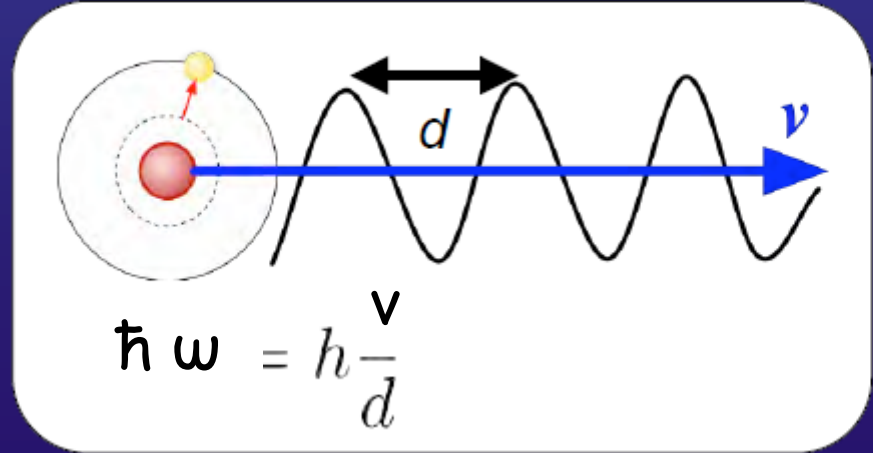


1s QED in $U^{91+} \approx 500\text{eV} \rightarrow$ measure M of U^{92+} to U^{91+} to U^{90+} to $4 \cdot 10^{-12}$ (in relative measurement) $\rightarrow$ QED to $<1\text{eV}$ to check high field and higher order

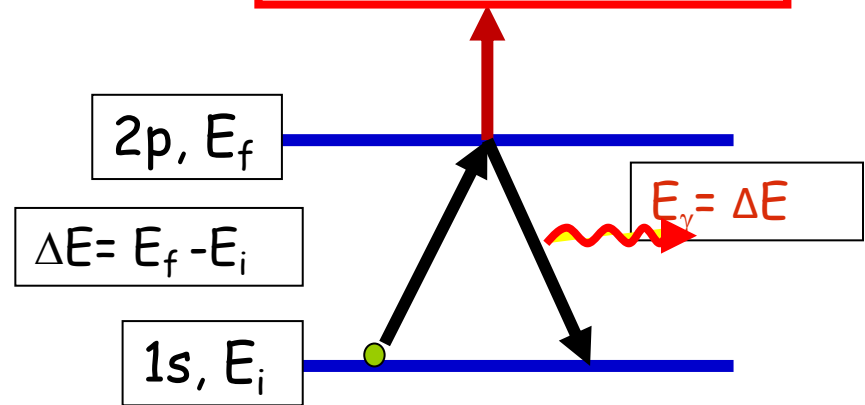
Precision Spectroscopy of 1s of Heavy Ion at High Energies GeV/u



Ion moving in a periodic crystal potential



Measurement with H-like Ion
enhanced ionisation



T. Azuma, et al.

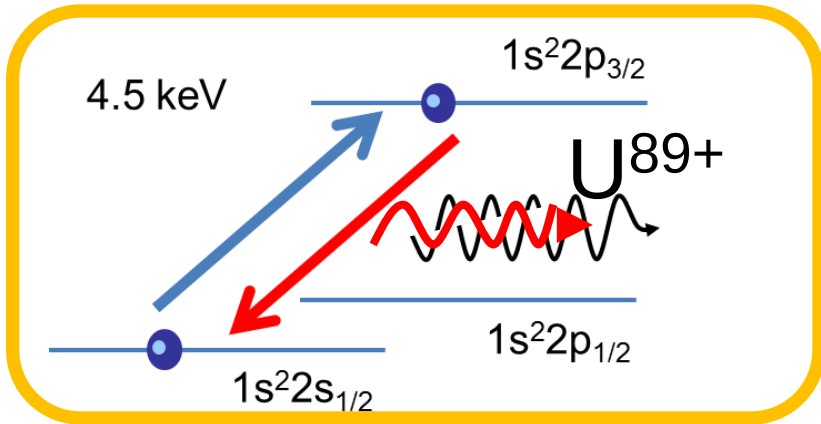
$$\Delta E = \frac{\gamma \hbar n v}{a} \left(\frac{k \cos \theta}{A} + \frac{l \sin \theta}{B} \right)$$

n order, γ Lorentz factor, a, k, l, A, B lattice constant
these are known, θ measured $\rightarrow \Delta E$

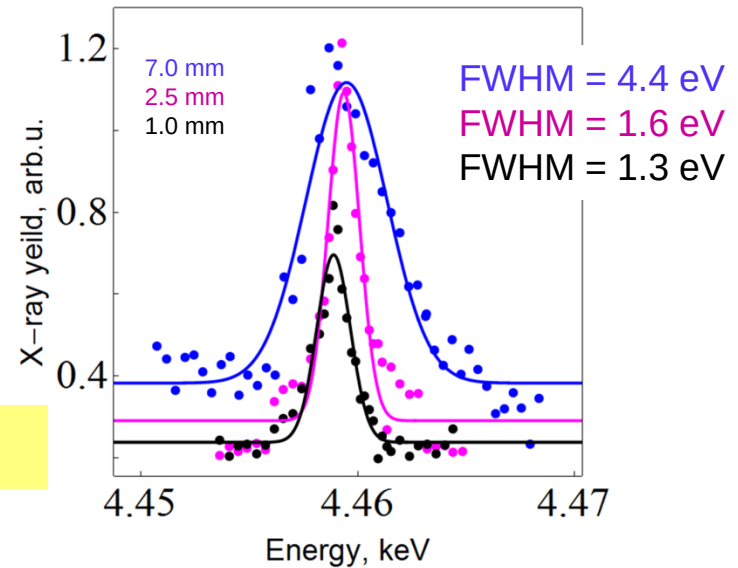
For relativistic ions, $v \sim 10^8$ m/s, $\gamma \approx 10$, and
atomic spacing 10^{-10} m, the oscillation
frequency is $\sim 10^{19} \text{s}^{-1}$ (100keV energy range)

Resonant Coherent Excitation at high energies (test with Li-like U @SIS18/ESR)

Small Particle Physics Research Collaboration



300 MeV/u U^{89+} in Si crystal



Only moderate beam intensities are required !

major factors determining the resolution:

Momentum spread of ion beam $\Delta p/p$: $\sim 10^{-5} - 10^{-4} \rightarrow$ fraction of eV

Energy loss of ions in target: $10 \text{ MeV}/(\text{mg}/\text{cm}^2) \rightarrow 1.4 \cdot 10^{-4} \cdot \text{Thickness } (\mu\text{m})$

Number of atoms rows inducing the excitation: 1.6×10^{-5}

Life time of the excited state: 1×10^{-14}

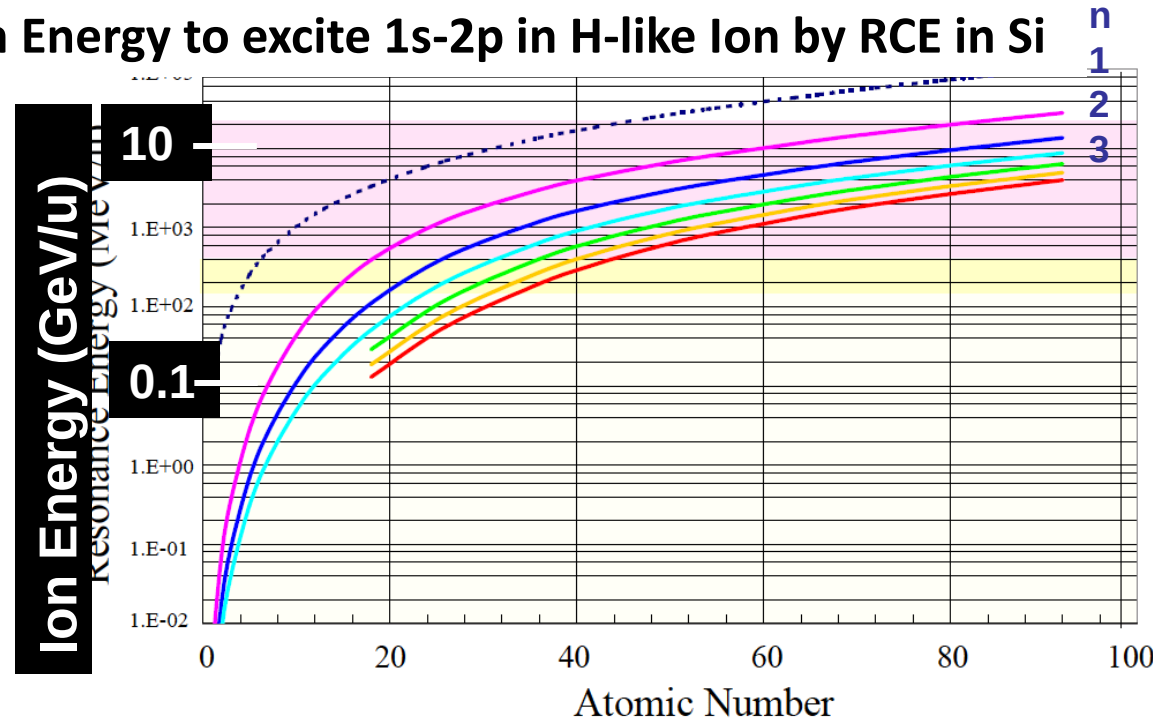
$$\rightarrow \Delta E(v, \theta) / E(v, \theta) \sim \Delta v / v = \Delta p / p$$

Precision Spectroscopy of 1s of Heavy Ion at High Energies GeV/u

at SIS 100 relativistic
ions $\gamma \rightarrow 10$, Z and q
up to 92
RCE proposal Azuma et
al. GSI, RIKEN



Ion Energy to excite 1s-2p in H-like Ion by RCE in Si



Issues to be solved: Beam cooling at 10 GeV/u
(laser cooling?)

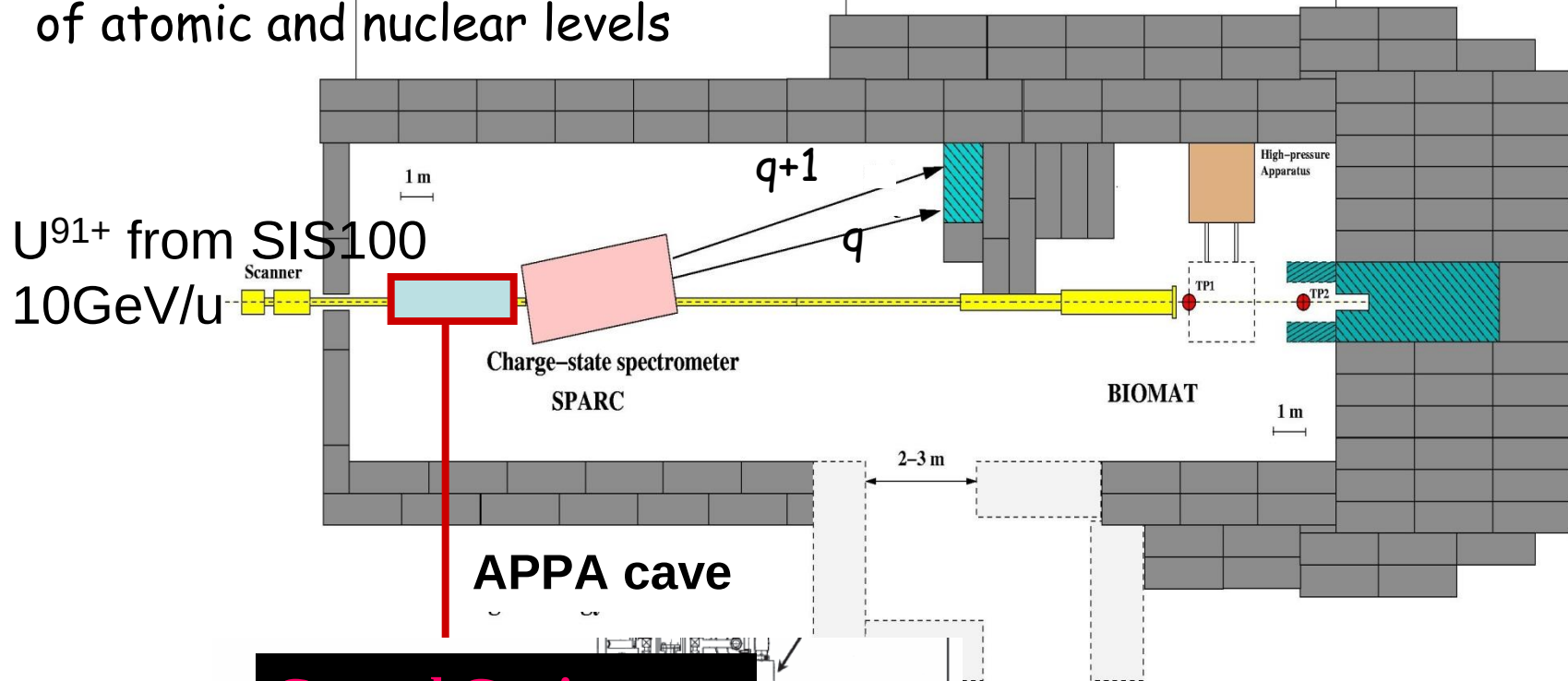
Energy loss at 10 GeV/u (probably reduced?)

maybe $\Delta E/E \approx 10^{-5} \rightarrow 1 \text{ eV of } 450 \text{ eV} \rightarrow$

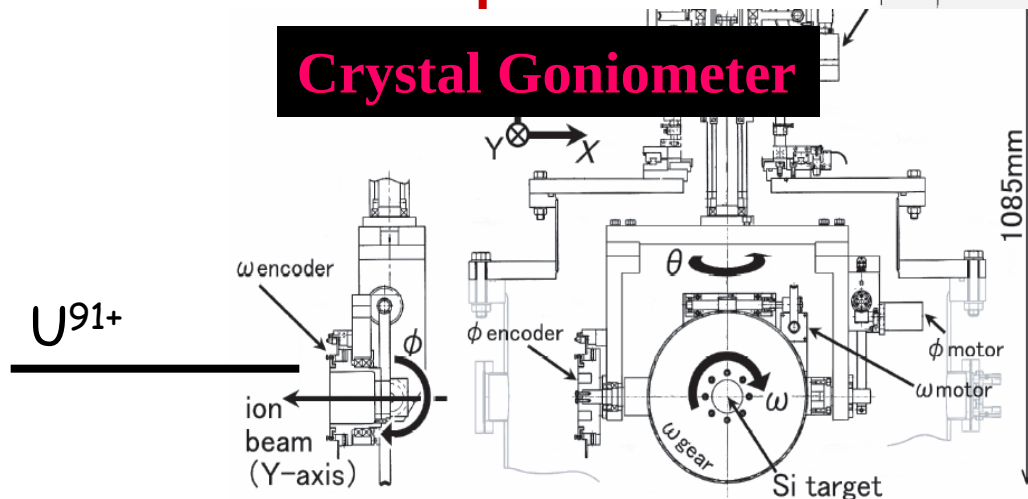
10^{-2} of Lamb-shift in U^{91+}

For U^{91+} we need the APPA cave and SIS100 FAIR

Precision spectroscopy by means of Resonant Coherent Excitation of atomic and nuclear levels



Crystal Goniometer

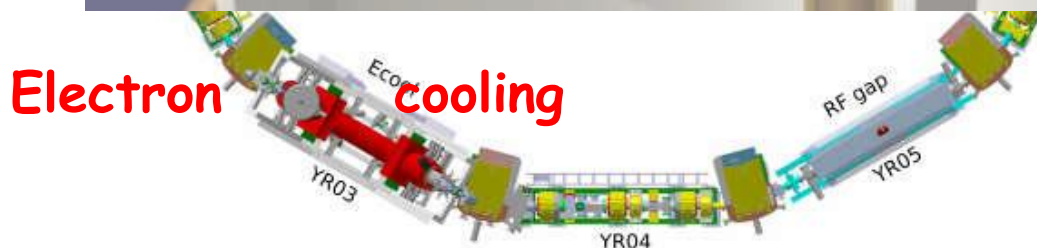
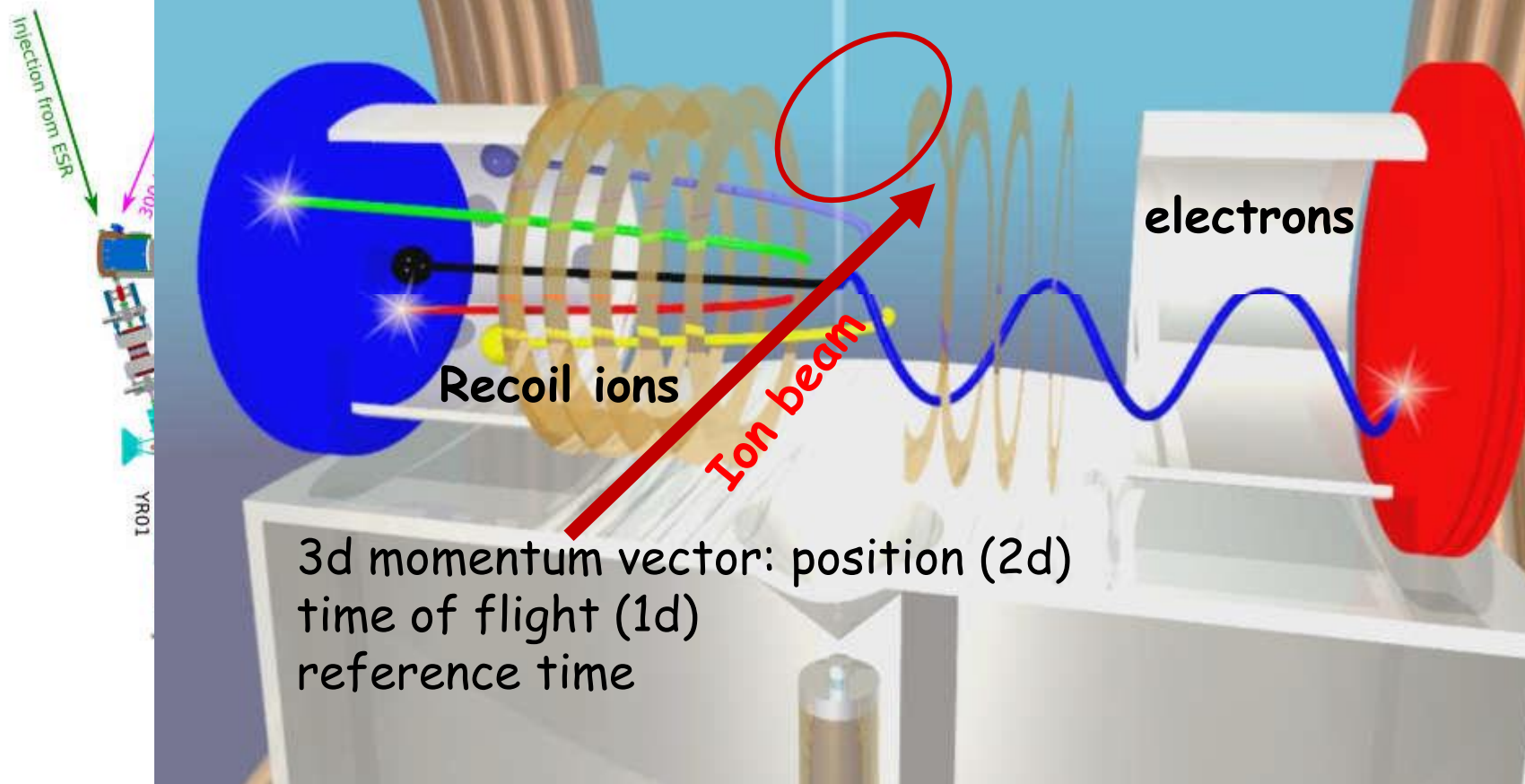


spare
Small Particles Atomic Physics Research Collaboration

T. Azuma, A. Bräunig-Demain, et al.

Collision
using

COLTRIMS: the reaction microscope



CRYRING@ESR



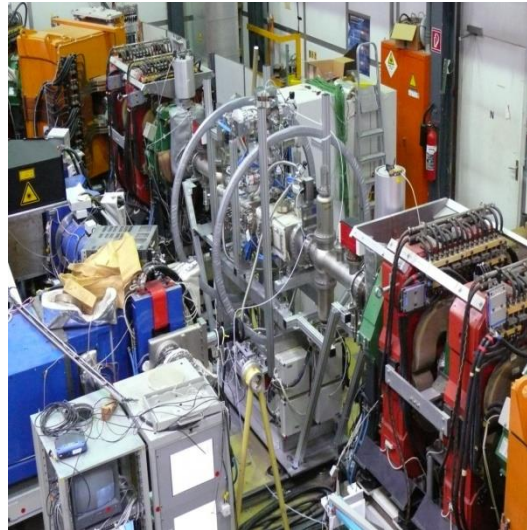
Collision Spectroscopy on Highly-Charged Ions using Ion Storage Ring and COLTRIMS

CRYRING@
Stockholm RIMS



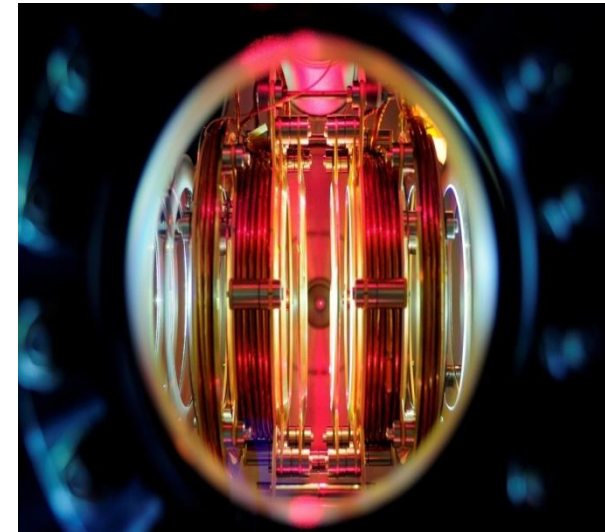
commissioned 1997

TSR, Heidelberg
ion-electron coincidences



commissioned 2009

TSR, Heidelberg
Ion-electron coincidence
optically trapped target



commissioned 2011

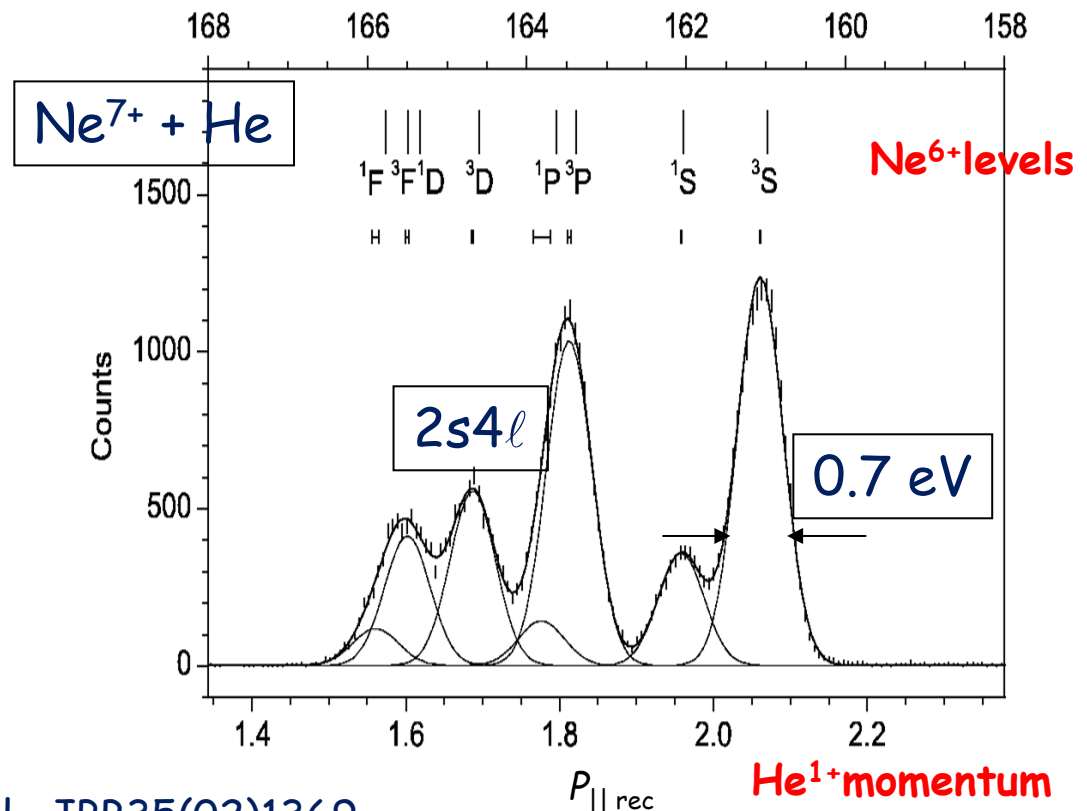
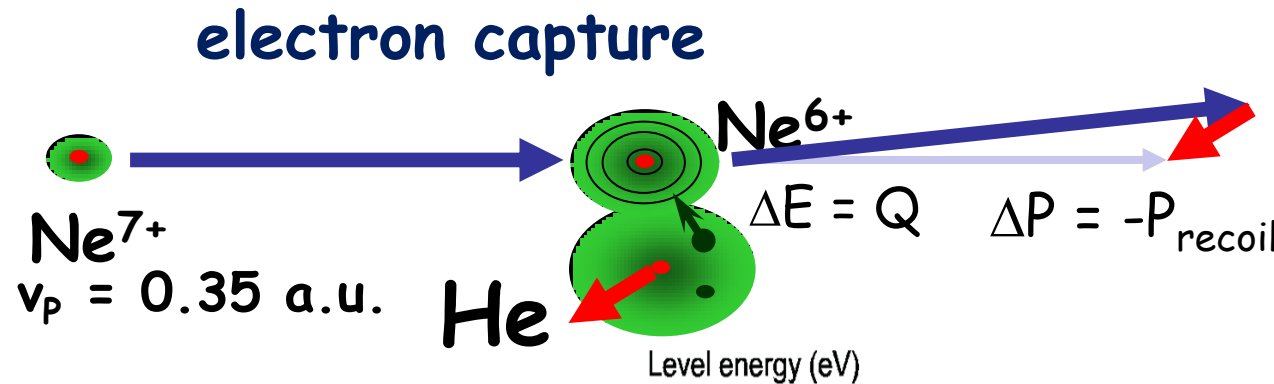
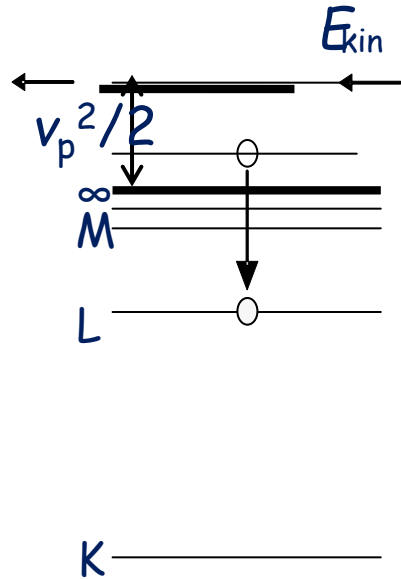
H. Schmidt et al., Phys. Rev. Lett. 89, (02), 163201

K. Schneider et al., Phys. Rev. Lett. 110 (11), 113201

R. Hubele, et al, Phys. Rev. Lett. 110 (13), 133201

Coming soon: Next generation COLTRIMS at CRYRING@ESR
(M. Schöffler, D. Fischer et al., Uni Frankfurt/Rolla)

Collision Spectroscopy on Highly-Charged Ions



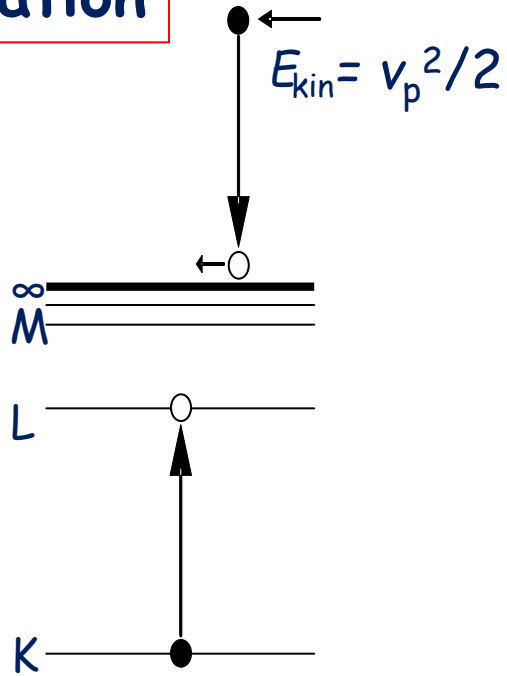
Advantages:

- 4π solid angle
- no selection rules, direct energy determination
- Energy precision ~ 1 meV

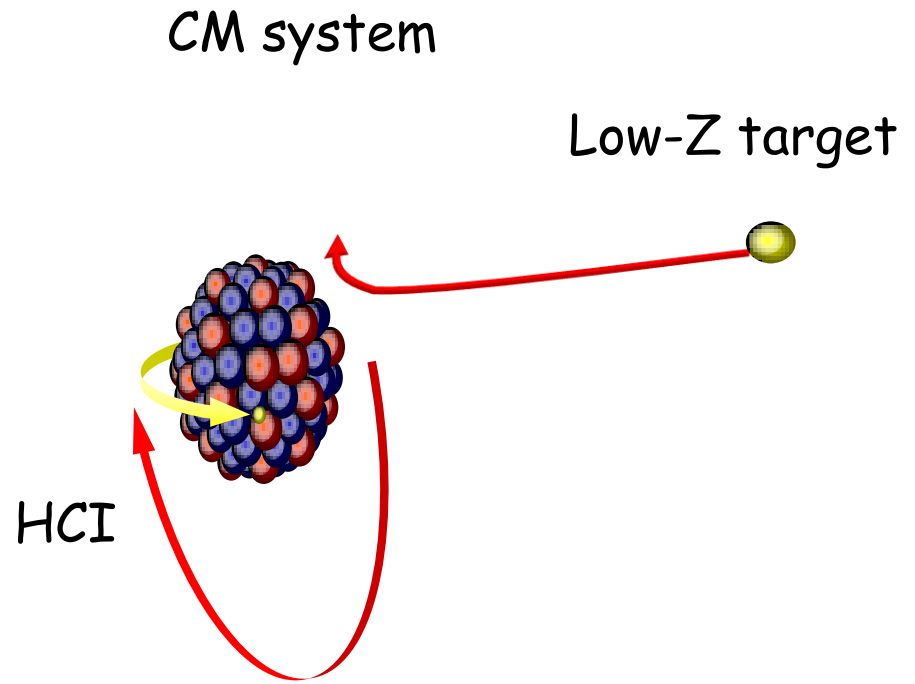
$$\Delta E_{kin} = \Delta E_{Bind}$$

Collision Spectroscopy on Highly-Charged Ions

excitation

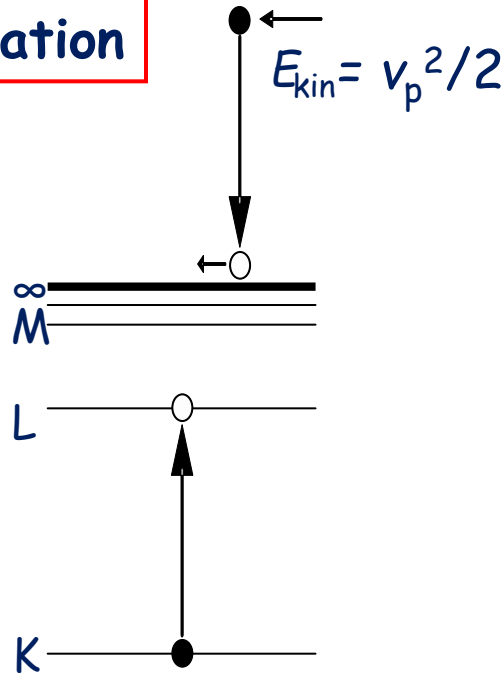


$$\Delta E_{\text{kin}} = \Delta E_{\text{exc}}$$



Collision Spectroscopy on Highly-Charged Ions

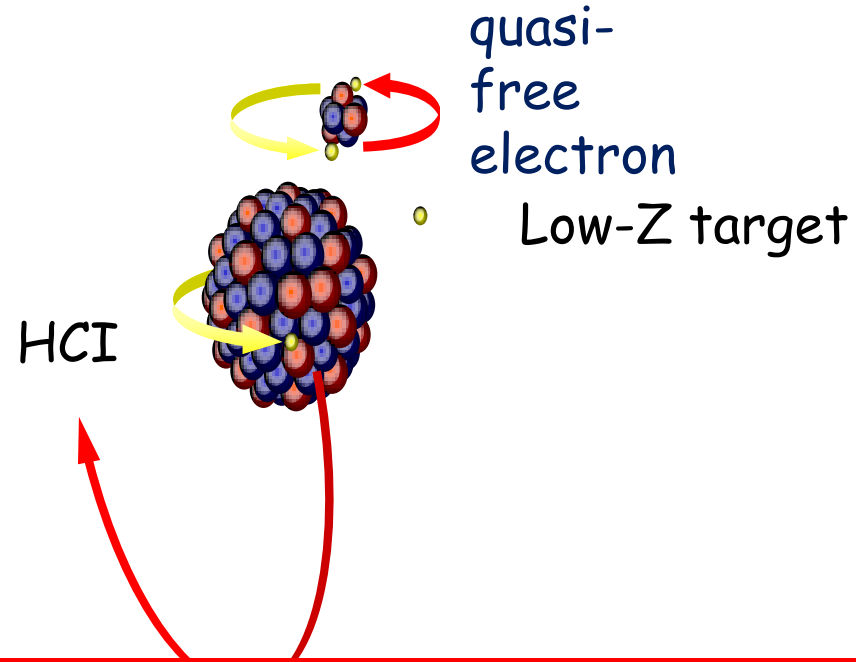
excitation



$$\Delta E_{\text{kin}} = \Delta E_{\text{exc}}$$

New technique with:

- 4 π solid angle acceptance
- excellent energy resolution
- all ionic states: $Z_p \leq 92$



Example: Xe^{53+}

$1s_{1/2} - 2p_{1/2}$ exc. energy $\sim 31 \text{ keV}$
 $2p_{1/2} - 2p_{3/2}$ splitting $\sim 430 \text{ eV}$
cross section $\sigma \sim 10^{-23} \text{ cm}^2$

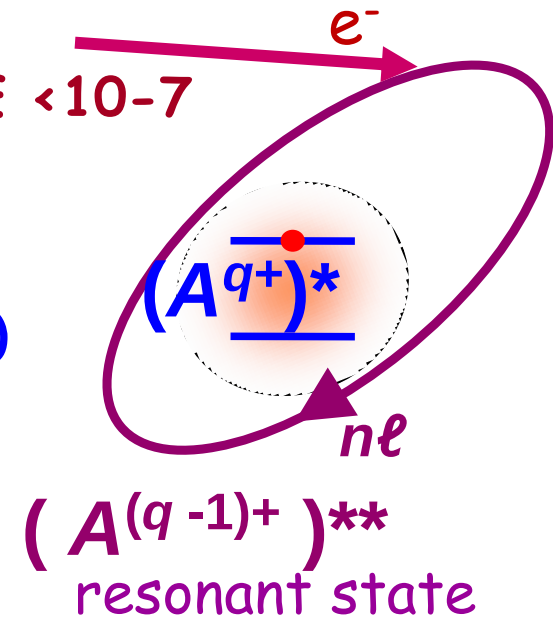
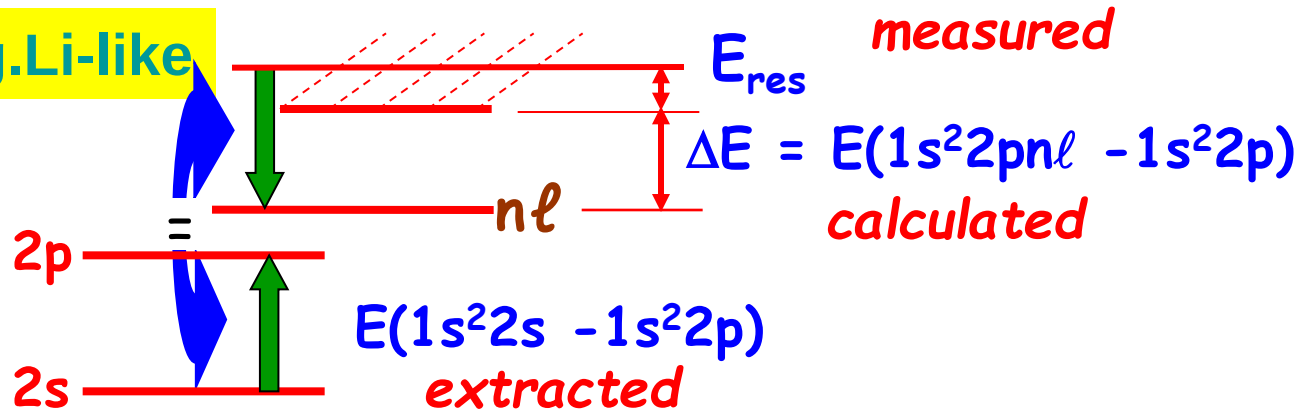
recoil momentum resolution $< 0.01 \text{ a.u.}$
energy resolution $< 10 \text{ eV}$

Collision Spectroscopy by Electron-Ion Recombination

Test QED in many e^- environment, e^- correlation, nuclear properties
(Hyperfine Interaction, Nuclear Size,....)

Method: $E_{\text{res}} = \Delta E - E_{nl} \approx 0 \Rightarrow \Delta E$ with $E_{\text{res}} / \Delta E < 10^{-7}$

e.g. Li-like

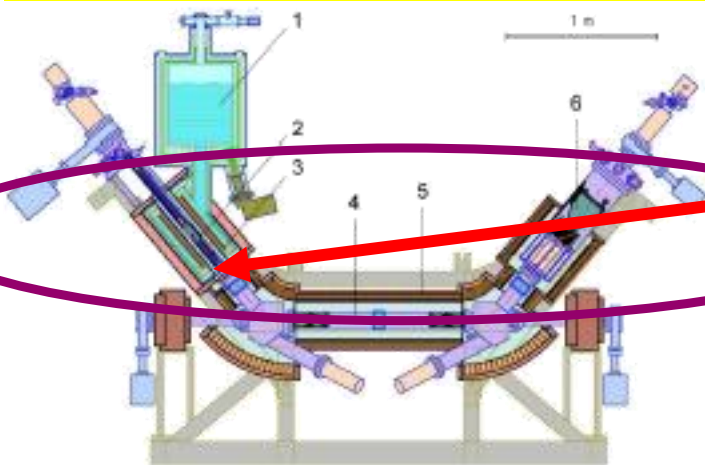


Calculate E_{nl} with e.g. Relativistic Many-Body Perturbation Theory (RMBPT) to any accuracy

Examples medium-Z (Kr^{33+}) and high-Z (Pb^{53+} , Pb^{78+}) ions

Important Ingredients: Storage Ring for Ions and Electron Cooler/Target

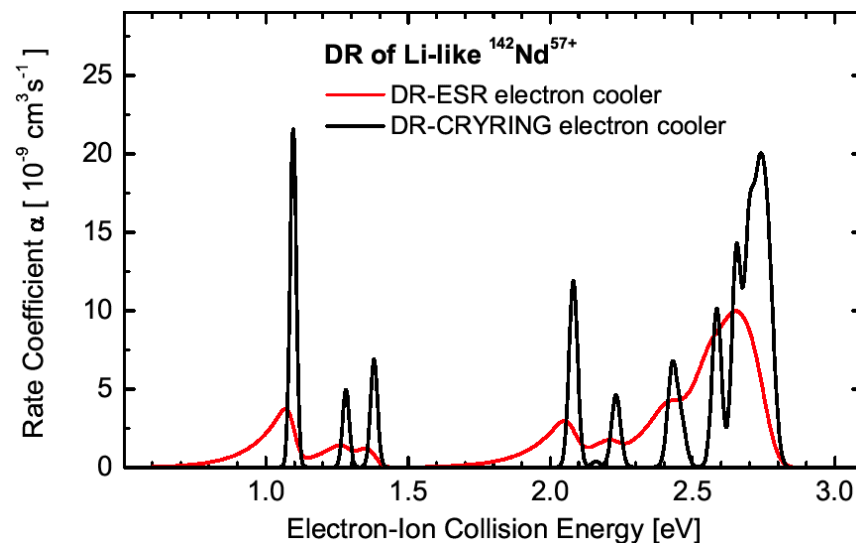
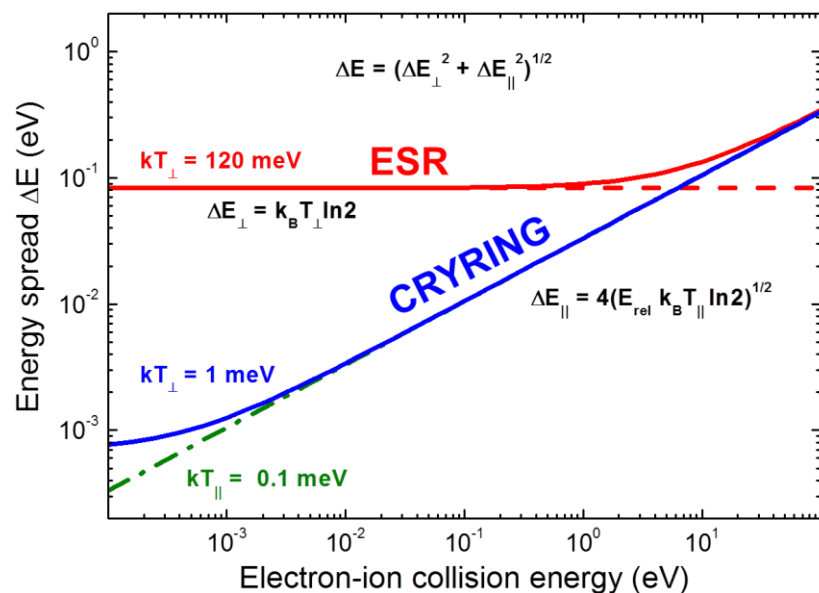
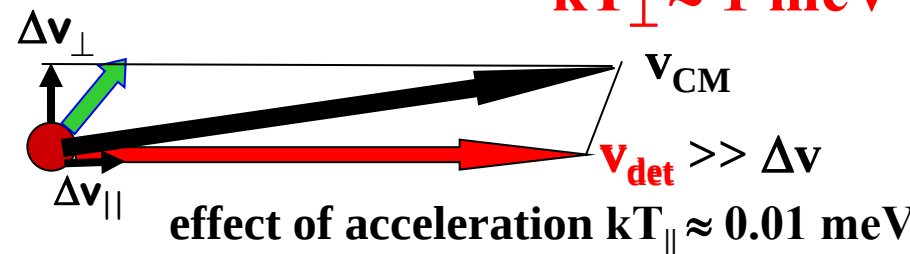
CRYRING + Electron Cooler



$$kT_{\perp} = 100 \text{ meV}$$

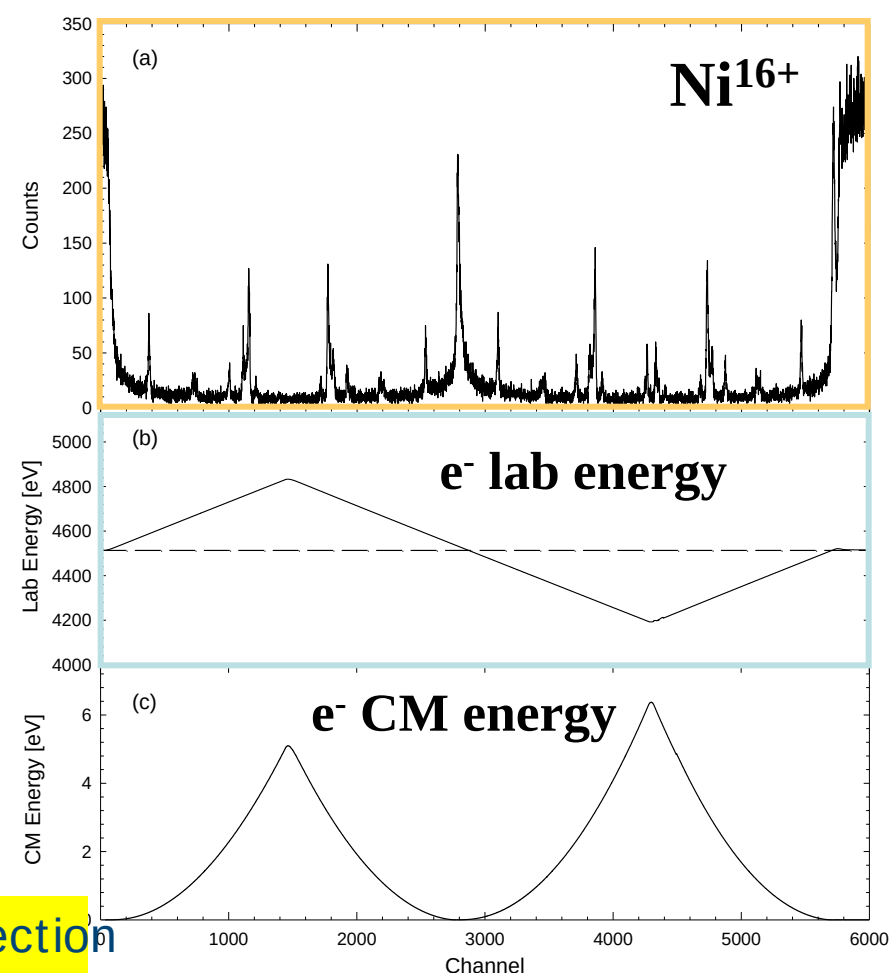
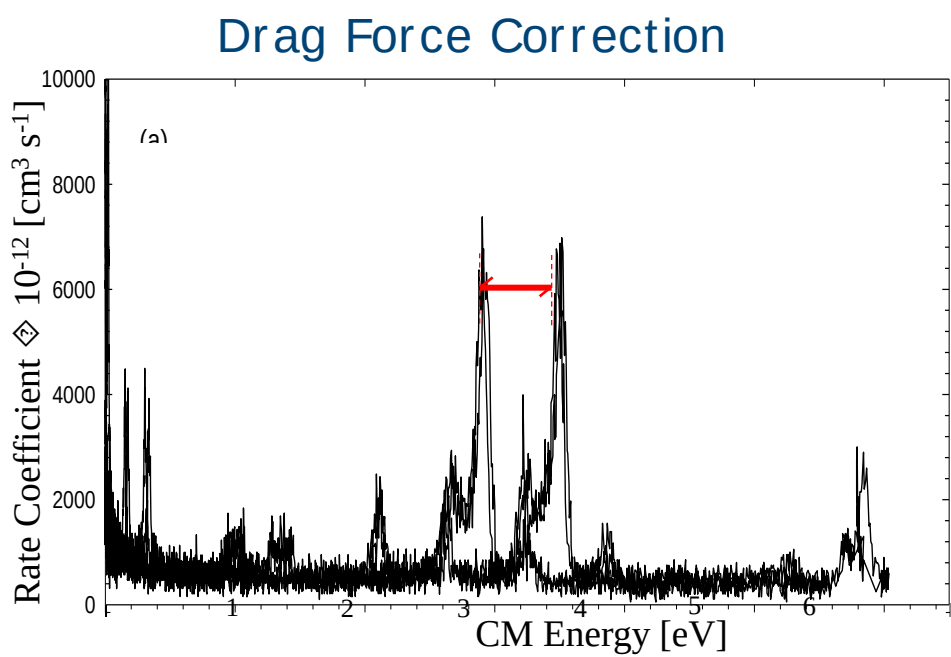
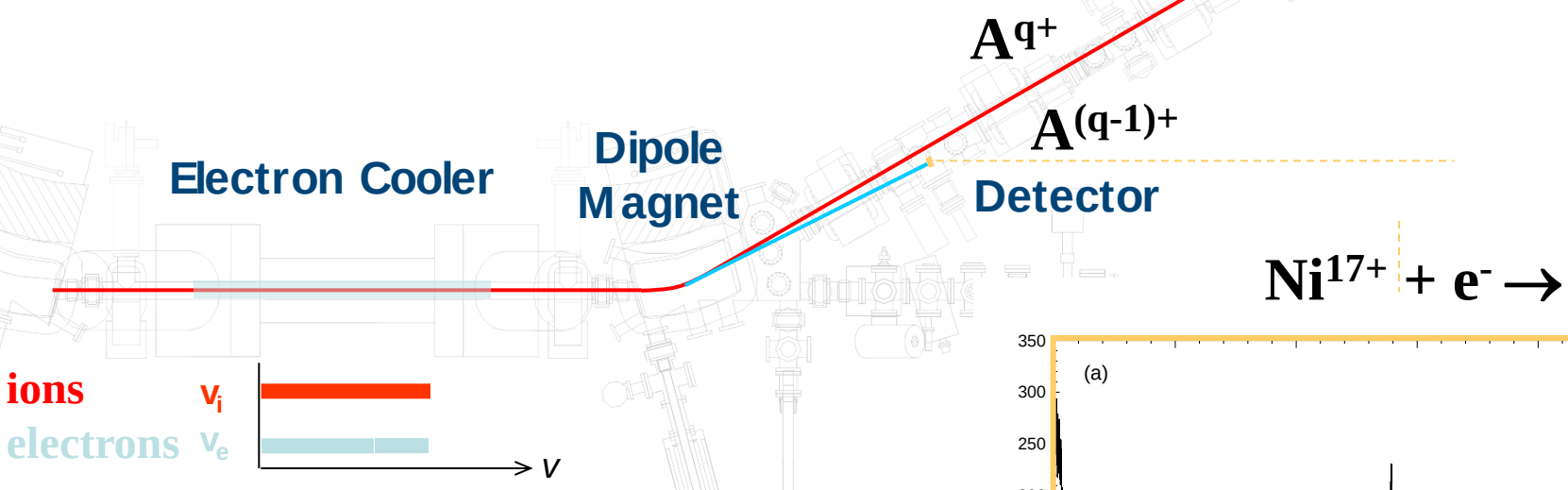
$$B_{\text{gun}} = 100 \times B_{\text{sol}}$$

$$kT_{\perp} \approx 1 \text{ meV}$$

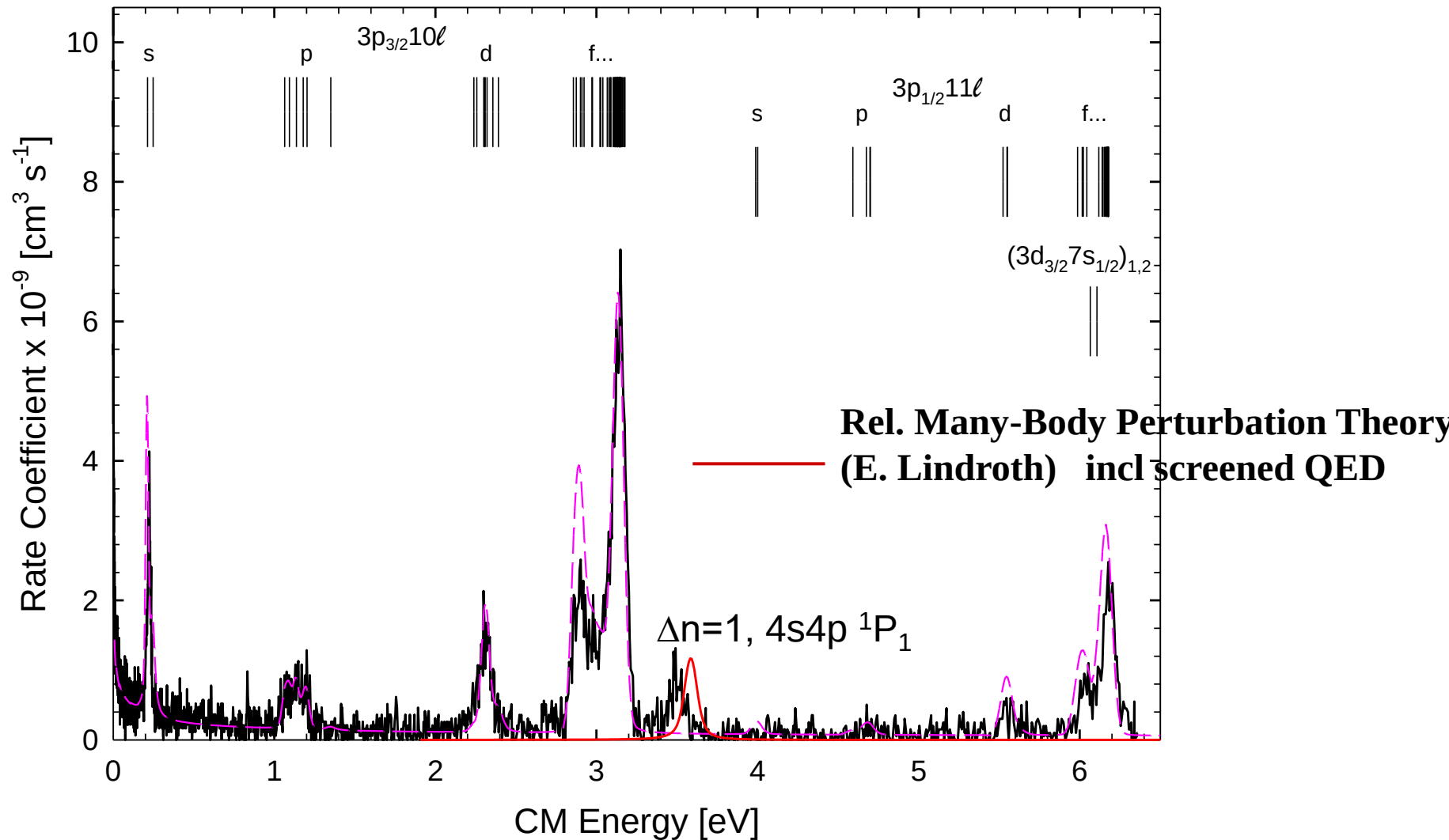
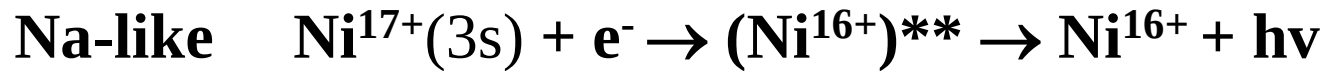


Great physics opportunities in CRYRING using beams from the ESR

CRYRING@Stockholm Experimental Method



Electron gun voltage + Space Charge Correction



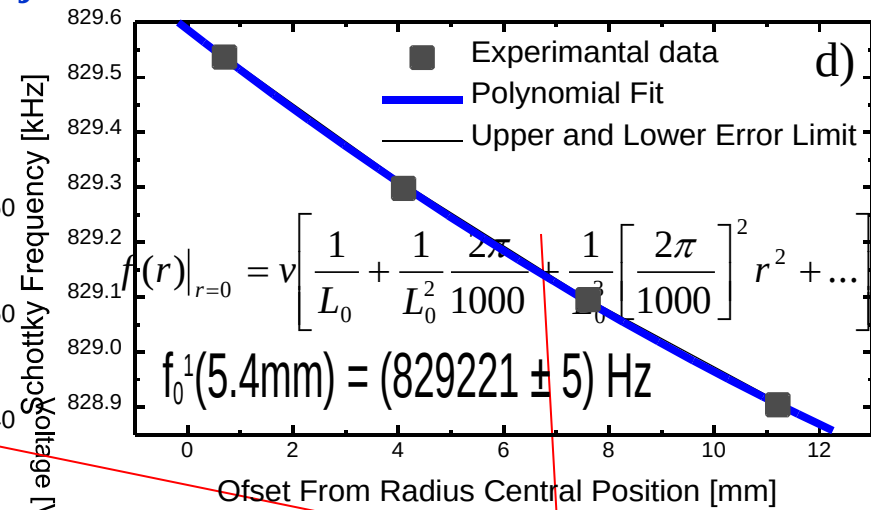
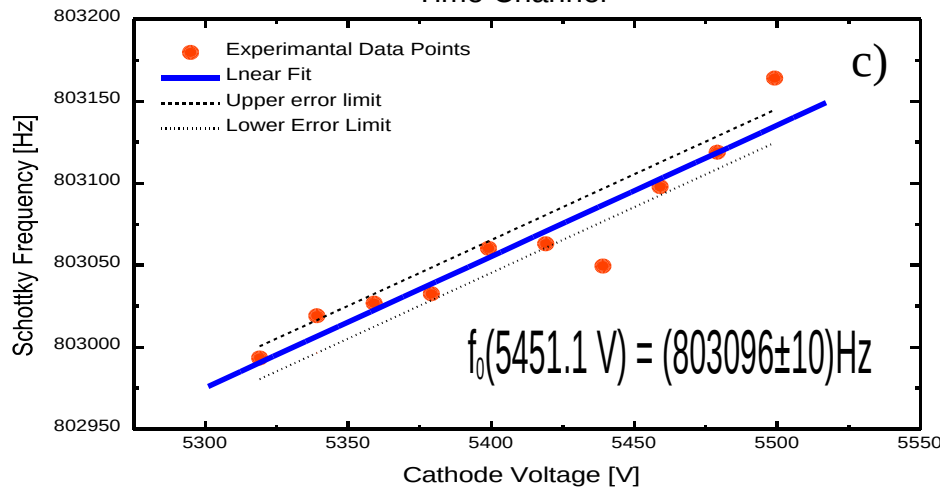
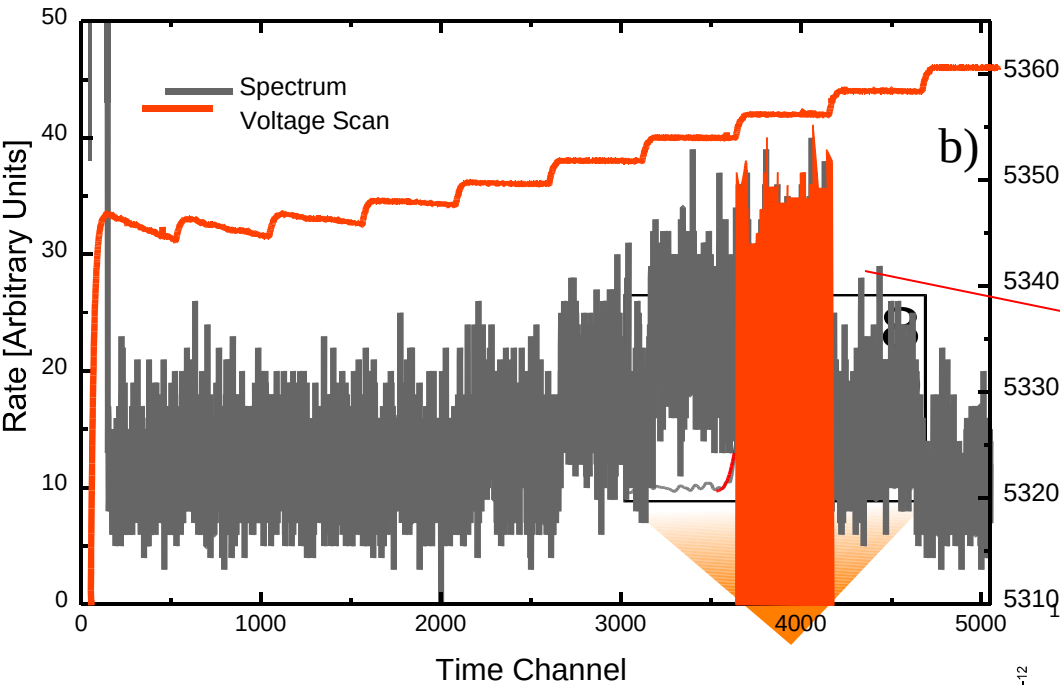
Estimated accuracy of the center of mass electron energy scale $\delta E/E \approx 10^{-2}$
 Method to improve the center of mass electron energy calibration by
 Schottky frequency and storage ring orbital length measurements:

Kr³³⁺

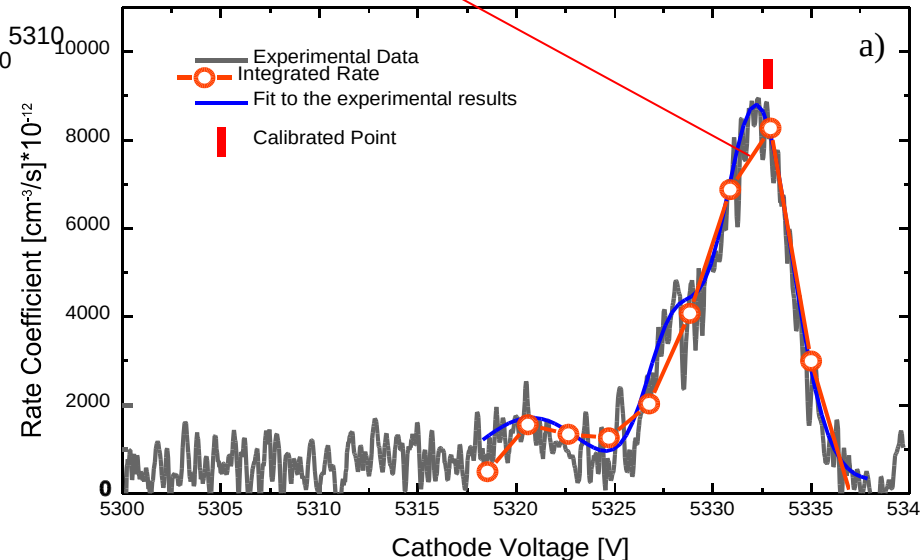


calibration by Schottky frequency

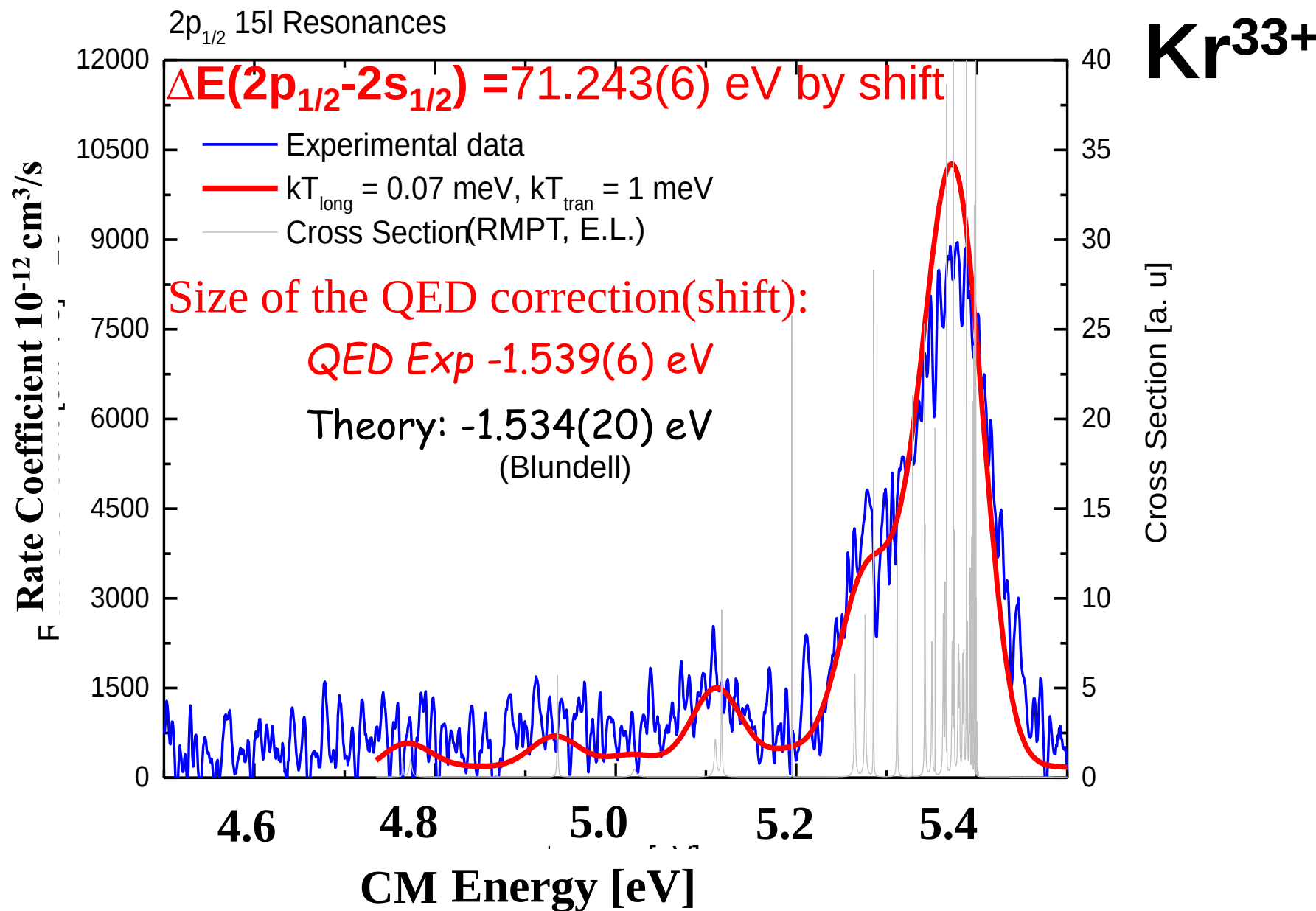
Scan over 5.37 eV resonance (2p_{1/2})



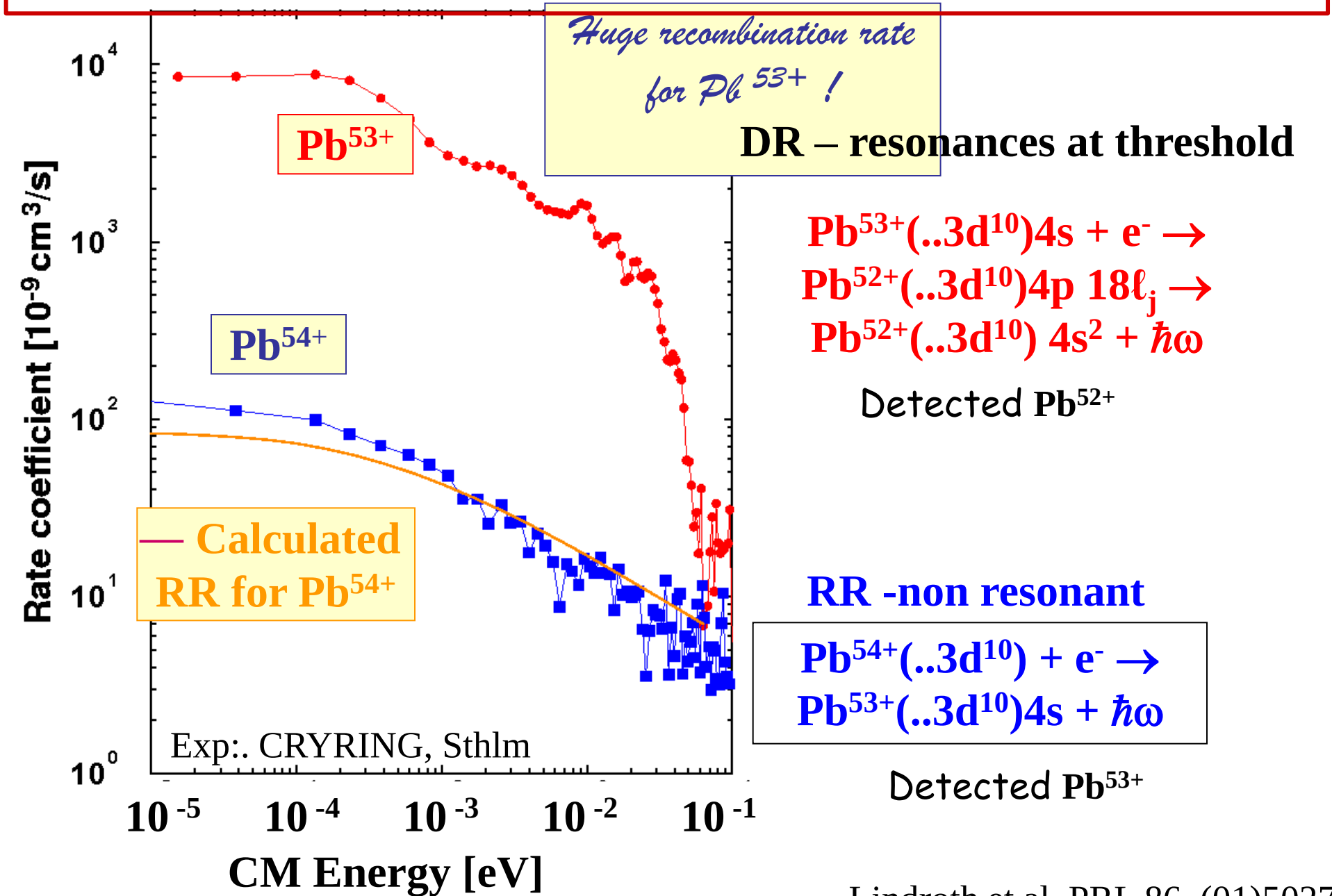
$$\Delta V = (f_0^1 - f_0) L$$



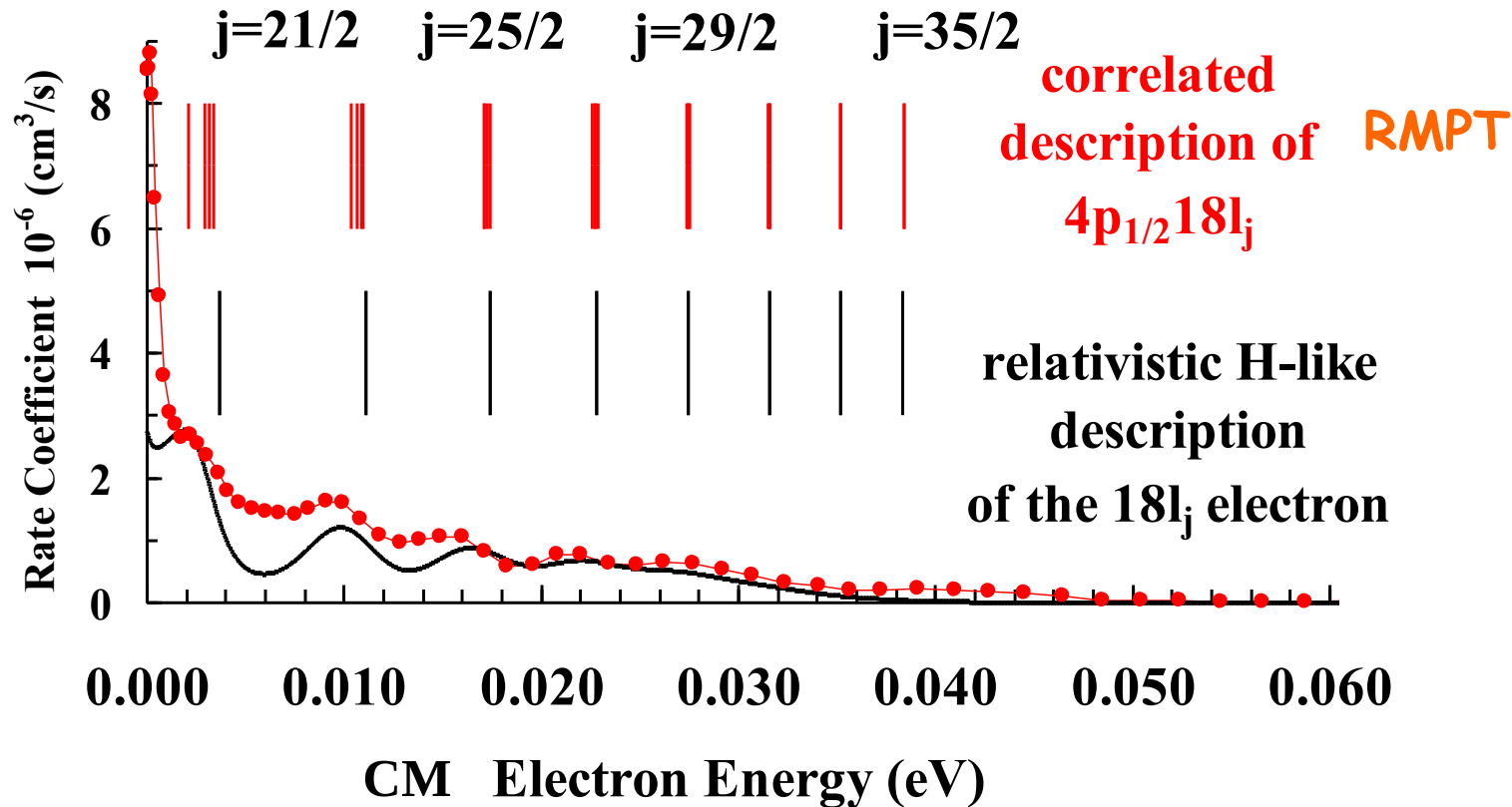
Collision Spectroscopy by Electron-Ion Recombination



Collision Spectroscopy by Electron-Ion Recombination



$$\varepsilon = \text{Pb}^{52+} (4p_{1/2} \text{ } 18l_j) - \text{Pb}^{53+} (4s_{1/2}) \approx \text{Pb}^{53+} (4p_{1/2} - 4s_{1/2}) + \Delta E(18l_j)$$



Had to shift RMPT resonances for QED in Pb^{53+}

Rate coefficient [arbitrary units]

Shift the threshold and
check agreement:

Best fit

first resonances: $4p_{1/2}18\ell_{21/2}$

Shift RMPT resonances
for QED in $P_{\ell} 53+$

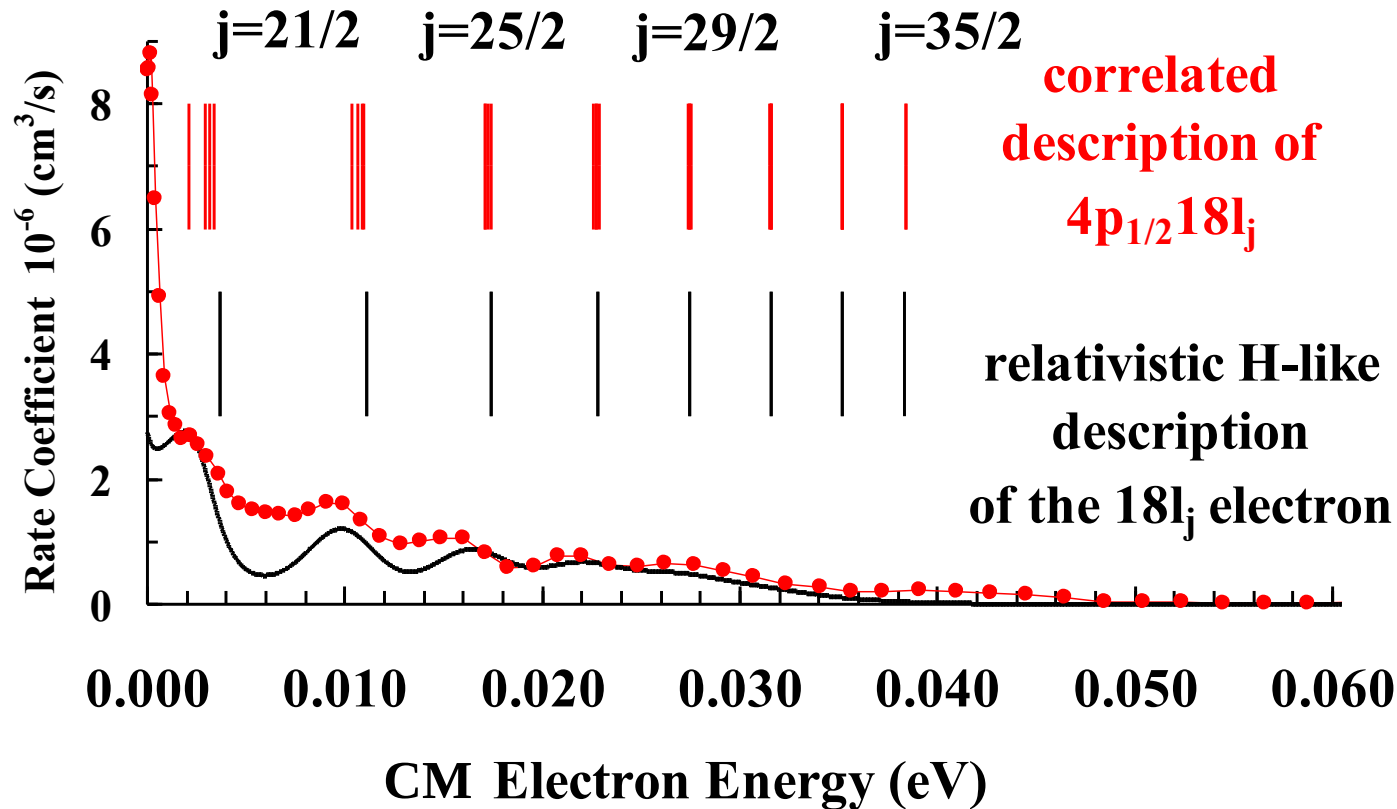
first resonances: $4p_{1/2}18\ell_{19/2}$

first resonances: $4p_{1/2}18\ell_{17/2}$

0 0.02 0.04 0.06

CM Electron energy [eV]

$$\varepsilon = \text{Pb}^{52+} (4p_{1/2} \text{ } 18l_j) - \text{Pb}^{53+} (4s_{1/2}) \approx \text{Pb}^{53+} (4p_{1/2} - 4s_{1/2}) + \Delta E(18l_j)$$



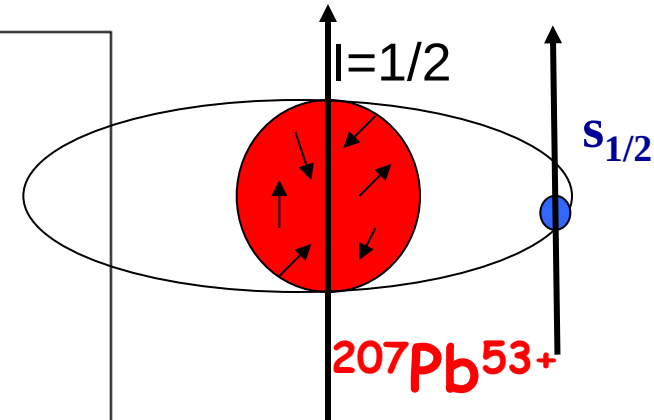
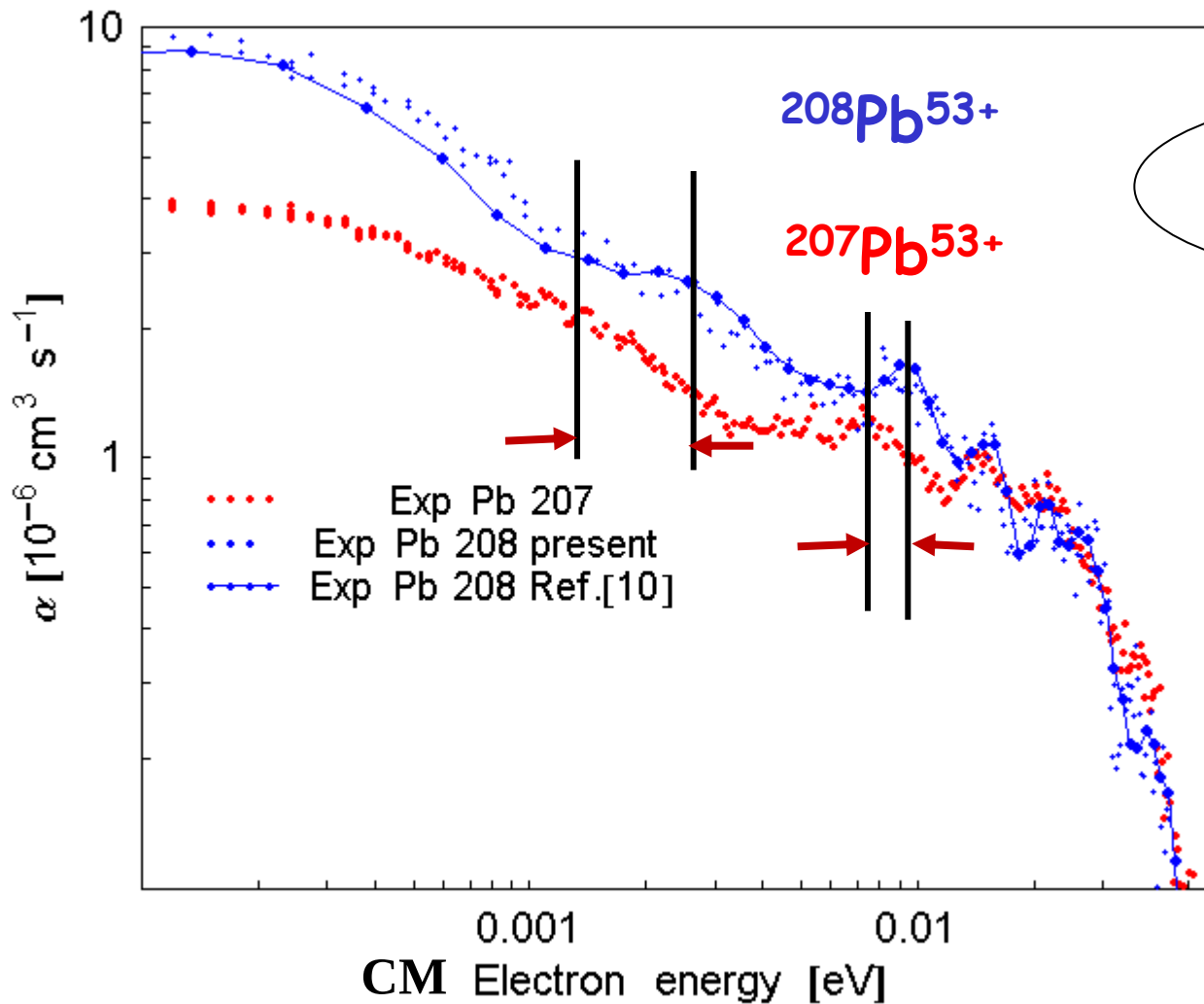
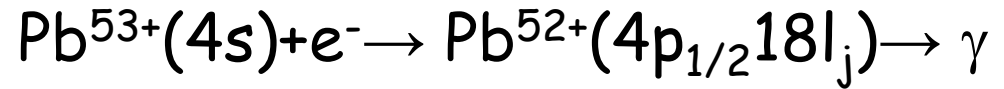
From QED correction adjusted so theoretical spectrum best fit experiment

$$\Rightarrow \text{Pb}^{53+} \Delta E (4s_{1/2} - 4p_{1/2}) = 118.010(1) \text{ eV rel. uncertainty } 8 \cdot 10^{-6}$$

QED part is: $-2.044(1) \text{ eV}$ (from exp.)

• Theoretical values: $-2.008(40) \text{ eV}$ (P. Indelicato) $-2.05(1) \text{ eV}$ (Blundell)

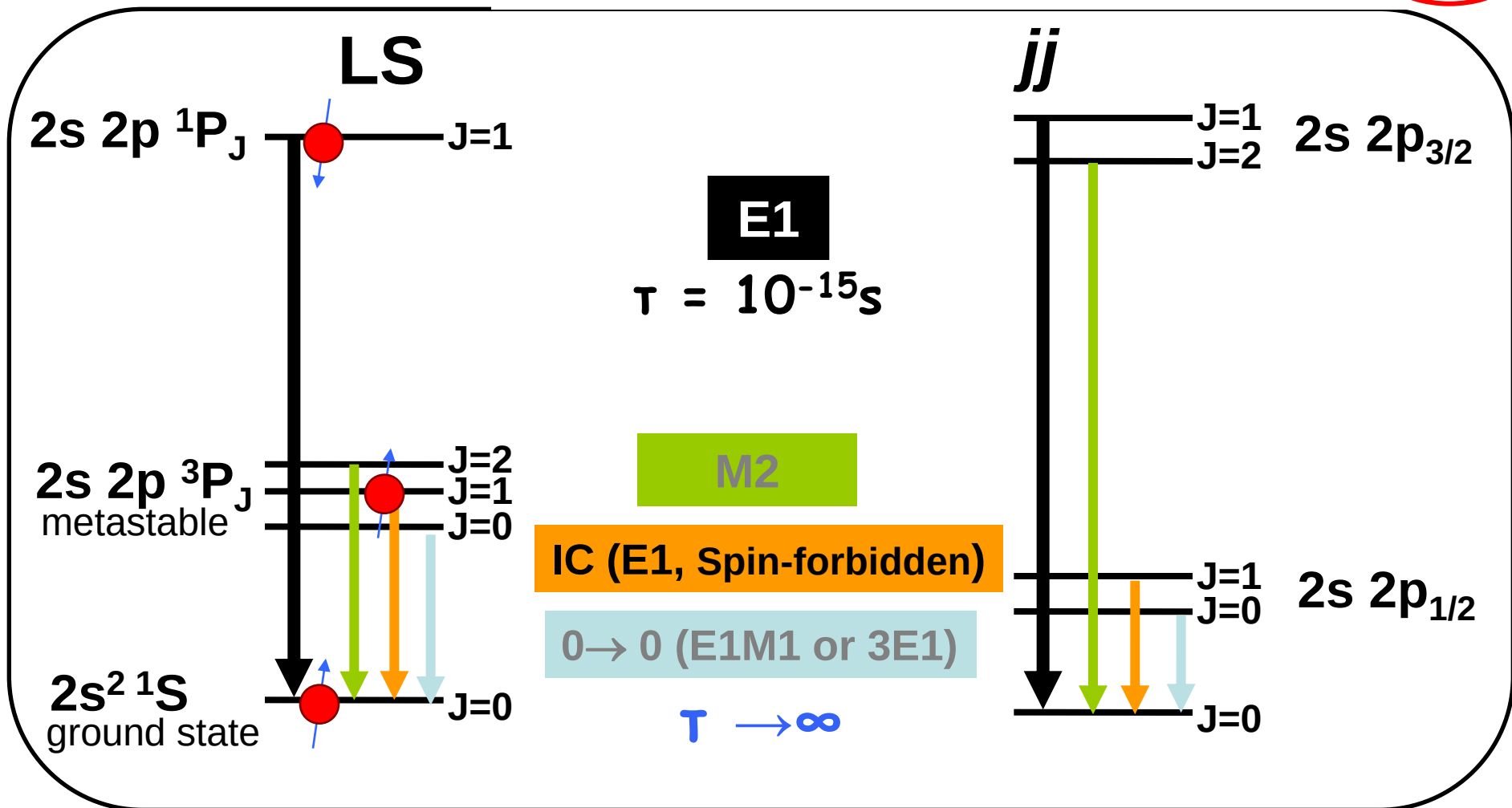
Hfs seen by DR!



exp. $\Rightarrow a = 4.6(3) \text{ meV}$
sensitive to nuclear
polarization (0.4) and
volume shift (1.6).

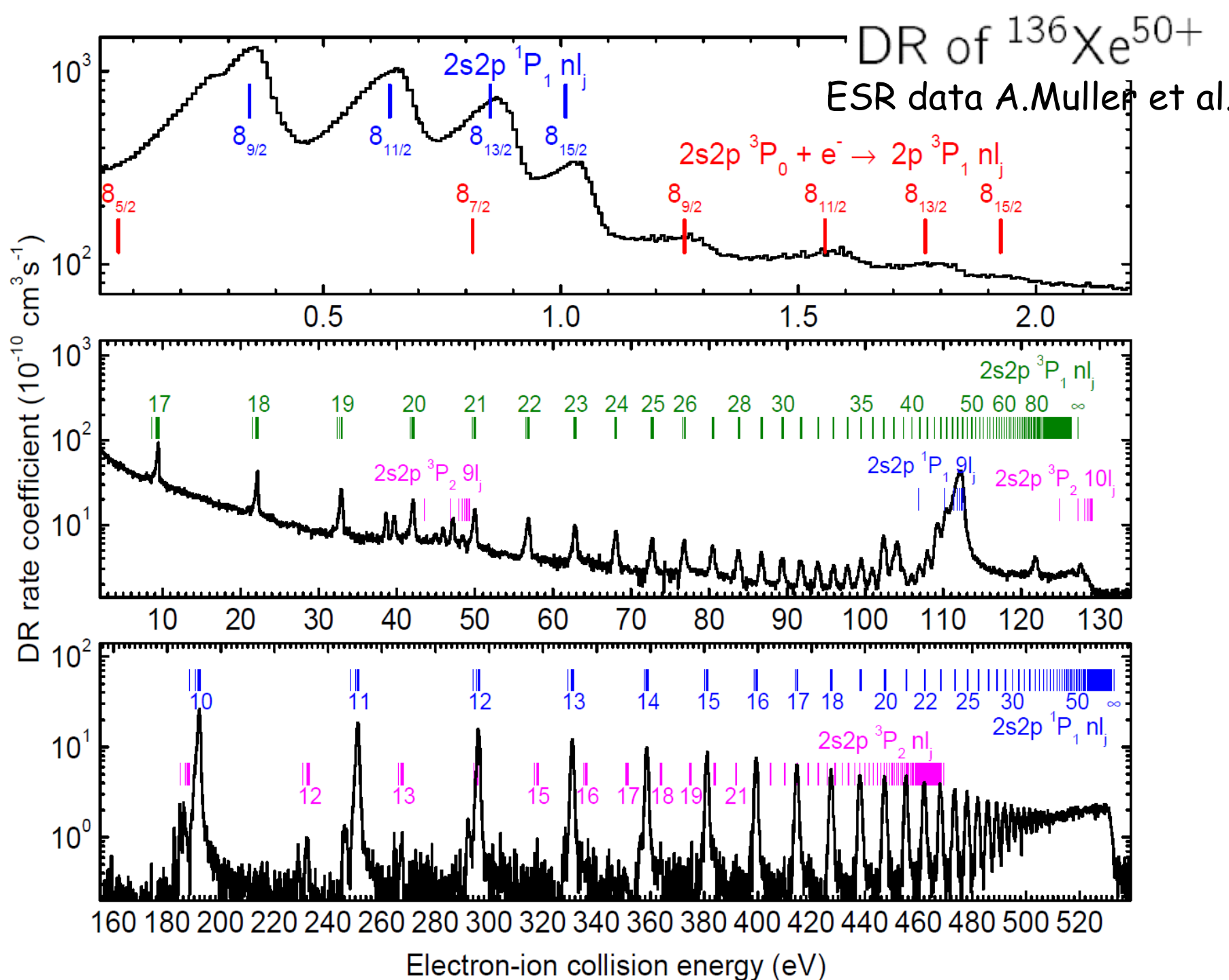
method attractive for radioactive beams,
needs low electron-beam energy spread!

Be-like Ions: Ne^{6+} , Si^{10+} , Ar^{14+} , Ti^{18+} , Kr^{32+} , Xe^{50+} , **Pb^{78+}**

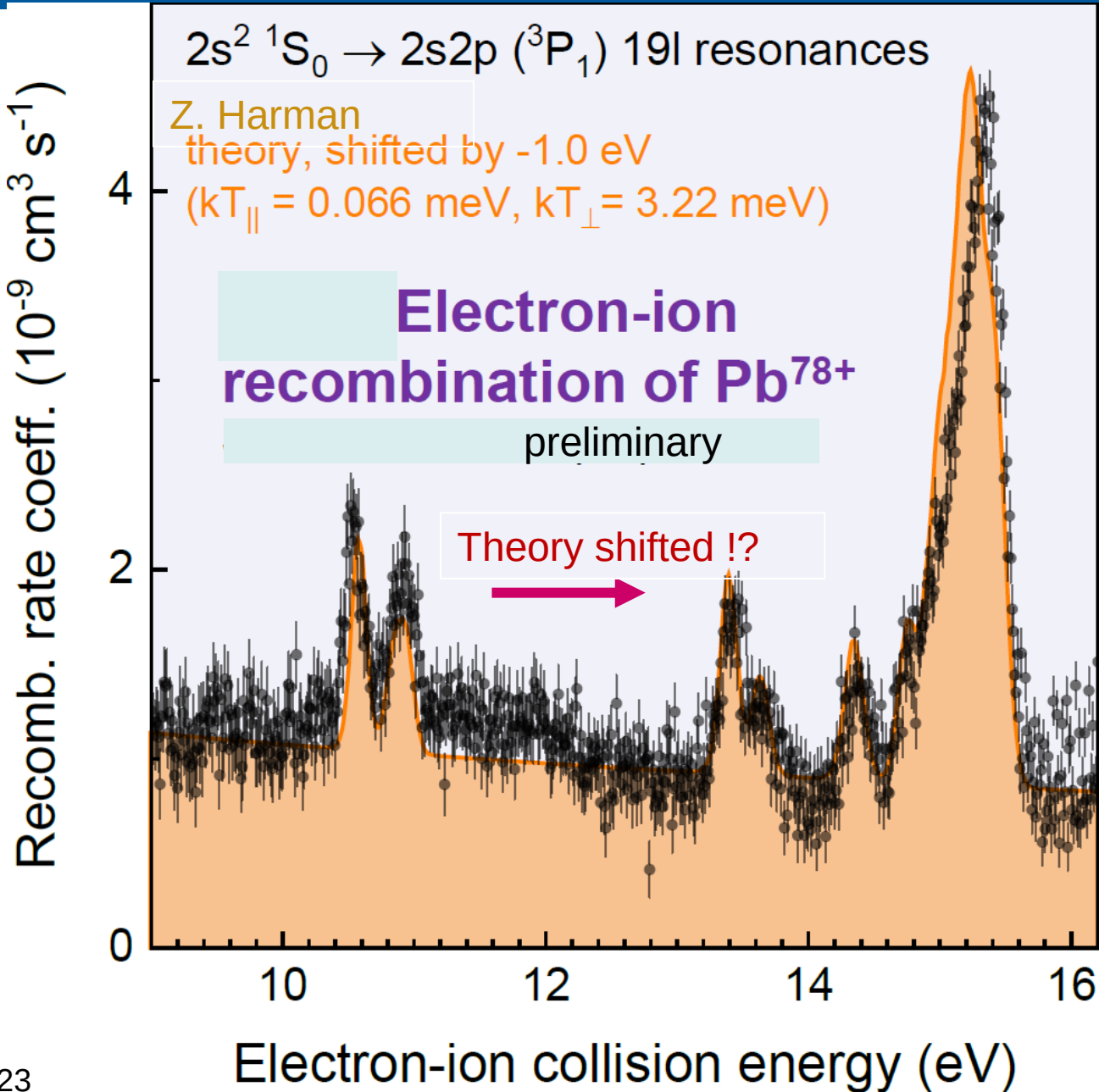
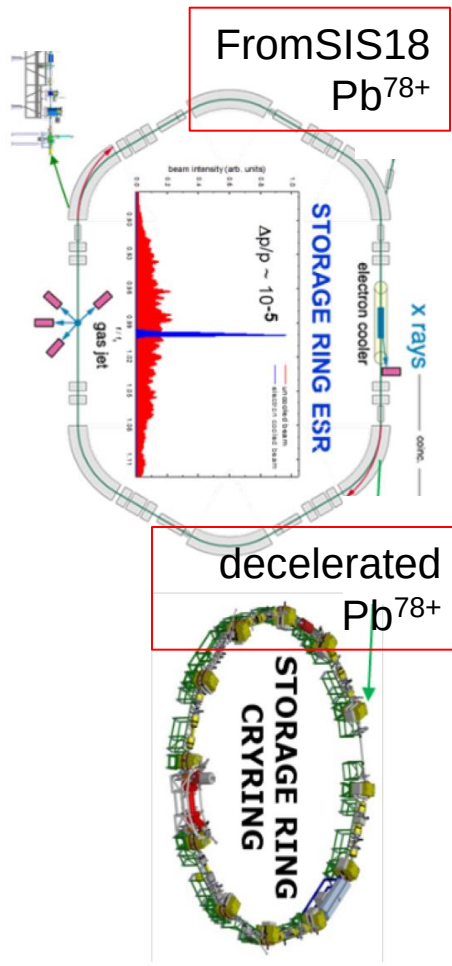


Possible
to study:

- lifetimes, energies to test atomic structure codes
- collisional & B- field quenching (astro & codes)
- breeding of metastable ions under controlled conditions



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to be publ.



Conclusions

- Spectroscopy in the dark can reach high precision and accuracy- compares well with photon spectroscopy
- Has several advantages and is complementary to photon spectroscopy:
- High detection efficiency, needs fewer ions (sometimes only one)
- Observes long lived states with traps (rings)
- Very clean experimental conditions (low background)
- Can be used to detect optically not allowed transitions

Many thanks to all collaborators over the years!

